

# CloudSat Project

A NASA Earth System Science Pathfinder Mission

## Level 2C Snow Profile Process Description and Interface Control Document

Product Version: P1\_R05

Document Revision: 0

Date: 1 May, 2018

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Citation:

Wood, N. B. and T. S. L'Ecuyer, 2018: Level 2C Snow Profile Process Description and Interface Control Document, Product Version P1\_R05. NASA JPL CloudSat project document revision 0., 26 pp. Available from [provide the URL from which this document was downloaded].

**Document Revision History**

<b>Date</b>	<b>Revision</b>	<b>Description</b>	<b>Sections(s) Affected</b>
1 May 2018	0	Initial Release	All

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# 1 Introduction

The CloudSat Snow Profile product (2C-SNOW-PROFILE) provides estimates of vertical profiles of snowfall rate along with snow size distribution parameters and snow water content for radar reflectivity profiles observed by the CloudSat Cloud Profiling Radar (CPR) which, based on an evaluation of the profile and ancillary data, appear to coincide with snow aloft producing precipitation (snow, mixed-phase precipitation, or rain) at the surface. For these profiles, if the surface precipitation type appears to be snow (dry snow or snow with only a small melted mass fraction), the product also estimates snowfall rate at the surface.

These estimated properties are obtained via an optimal estimation retrieval applied to radar bins in a profile that appear to contain snow and associated snow-producing cloud (the snow layer). The optimal estimation algorithm retrieves profiles of snow size distribution parameters using the snow layer reflectivity profile, ancillary meteorological information, and a priori information about snow microphysical properties, radar scattering properties, and size distribution parameters. Because of ground clutter, the CPR cannot reliably measure reflectivities near the surface. Due to this limitation, the base of the snow layer may be truncated somewhat above the surface to avoid ground clutter effects. The retrieved size distribution parameter profiles and the a priori information are used to calculate profiles of snowfall rates and snow water contents. The optimal estimation method produces uncertainty estimates for the retrieved size distribution parameters, and these uncertainties are then used to estimate uncertainties for the snowfall rates and snow water contents. If the surface precipitation type is snow, the surface snowfall rate is estimated using the snow properties at the base of the snow layer.

This document describes the algorithm that has been implemented in Release 5 (R05) of the 2C-SNOW-PROFILE product. For each radar profile, the algorithm examines variables from 2C-PRECIP-COLUMN to determine if precipitation is present at the surface and the precipitation phase. In cases where the 2C-PRECIP-COLUMN data are inconclusive, the algorithm examines the near-surface reflectivities and cloud mask from 2B-GEOPROF and temperatures from ECMWF-AUX to determine precipitation presence and phase. If precipitation is present, the algorithm

- examines the reflectivity and cloud mask profile from 2B-GEOPROF and the temperature profile from ECMWF-AUX to locate a snow layer: a contiguous range of radar bins which contain snow and snow-producing cloud;
- assigns a priori expected values, uncertainties and initial values to the snow size distribution parameters in each snow-containing radar bin in the snow layer;
- retrieves a profile of snow size distribution parameters and their uncertainties using the radar reflectivity profile in the snow layer;
- calculates a profile of snowfall rates, snow water contents and their uncertainties for the snow layer;
- and, if appropriate, estimates the surface snowfall rate and its uncertainty using the snowfall rate and its uncertainty from the base of the snow layer.

## 1.1 What's New: Product Version History

Changes from version P\_R04 to version P1\_R05 include:

- Snow retrievals are now also performed for snow above the melting level when rain or mixed-phase precipitation appear to be reaching the surface. This extends the behavior in prior version P\_R04, in which retrievals were performed only when snow appeared to be reaching the surface. See section 7 for an illustration of the new retrieval capabilities and section 8 for cautions about the use of these new data.
- The location in the snow layer of the -15 dBZe echo top is included in the product. The variable `snow_top_height_bin` gives the index of the radar bin where the reflectivity falls below -15 dBZe.
- The snow layer in which properties are retrieved now includes any contiguous radar bins immediately above the -15 dBZe echo top that appear to contain cloud-like reflectivities. These are radar bins with reflectivities smaller than -15 dBZe but larger than the radar minimum detectable signal and with cloud mask values

indicating the presence of cloud. The algorithm assumptions used in these cloud-like bins are the same as those used in the remainder of the snow layer.

## 2 Product Contents

The product is provided in HDF format, in files each of which contain both geolocation information and product data for a single orbit, or granule. Variables are dimensioned as scalars; as arrays of dimension  $N_{\text{ray}}$ , where  $N_{\text{ray}}$  is the number of vertical radar profiles measured during the orbit; or as arrays of dimension  $N_{\text{bin}} \times N_{\text{ray}}$ , where  $N_{\text{bin}}$  is the number of vertical radar bins in a profile.

### 2.1 Data fields

Data fields are tabulated in Table 1 and, except as noted, are produced by 2C-SNOW-PROFILE. Descriptions of the fields provided by 2C-SNOW-PROFILE follow. For other fields, see the documentation of the referenced products.

Table 1: 2C-SNOW-PROFILE data fields.

Variable	Dimension	Units	Description
Data_quality	$N_{\text{ray}}$	–	Flags indicating radar data quality (from 2B-GEOPROF)
Data_status	$N_{\text{ray}}$	–	Spacecraft data status flags (from 2B-GEOPROF)
Data_targetID	$N_{\text{ray}}$	–	CPR bus orientation (from 2B-GEOPROF)
snow_retrieval_status	$N_{\text{ray}}$	–	Retrieval status flags (see description below)
norm_chi_sq	$N_{\text{ray}}$	–	Retrieval normalized chi square
log_N0	$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{m}^{-3} \text{mm}^{-1})$	$\log_{10}$ of the snow size distribution intercept parameter, $N_0$
log_N0_uncert	$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{m}^{-3} \text{mm}^{-1})$	Uncertainty of $\log_{10}(N_0)$
log_lambda	$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{mm}^{-1})$	$\log_{10}$ of the snow size distribution slope parameter, $\lambda$
log_lambda_uncert	$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{mm}^{-1})$	Uncertainty of $\log_{10}(\lambda)$
snowfall_rate	$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$	Snowfall rate profile, $S$
snowfall_rate_uncert	$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$	Uncertainty of $S$
snowfall_rate_sfc	$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$	Snowfall rate at the surface, $S_{sfc}$
snowfall_rate_sfc_uncert	$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$	Uncertainty in $S_{sfc}$
snowfall_rate_sfc_confidence	$N_{\text{bin}}, N_{\text{ray}}$	–	Parameter indicating confidence in $S_{sfc}$ (see description below)
snow_water_content	$N_{\text{bin}}, N_{\text{ray}}$	$\text{g m}^{-3}$	Snow water content, $SWC$
snow_water_content_uncert	$N_{\text{bin}}, N_{\text{ray}}$	$\text{g m}^{-3}$	Uncertainty in $SWC$
snow_top_height_bin	$N_{\text{ray}}$	–	Index of bin containing snow echo top

**snow\_retrieval\_status** The retrieval status for each profile is represented by an 8-bit field, stored in the HDF file as a signed, 1-byte integer value in variable snow\_retrieval\_status. The interpretation of each bit is as follows:

**Bit 0:** (Least significant bit) A snow layer is detected in the profile. Detection is based on a combined evaluation of the reflectivities, cloud mask values and temperatures in the truncated profile.

**Bit 1:** Snow is indicated at the surface. For most profiles, this is determined by examining the variables Precip\_flag and Melted\_fraction from 2C-PRECIP-COLUMN. This flag is set if Precip\_flag indicates “Snow certain” or “Snow possible”, or if it indicates “Mixed certain” or “Mixed possible” with a value of Melted\_fraction

less than or equal to 0.1. Additionally, if the 2C-PRECIP-COLUMN variables are not conclusive, 2C-SNOW-PROFILE performs an independent evaluation. If snow is detected in the truncated profile, and the temperatures at the surface are sufficiently cold so that the melted mass fraction is less than or equal to 0.1, snow is indicated at the surface.

**Bit 2:** A retrieval was performed, but produced large chi-square values. This can be an indication the retrieval has converged to a state that is inconsistent with the observations or with the a priori assumptions, and suggests the results should be used with caution.

**Bit 3:** The snowfall rate at the base of the snow layer is substantially larger than that in the profile bin immediately above. This may be an indication of the effects of surface clutter, shallow precipitation, or partial melting of the snow, and suggests these results should be used with caution. See section 8 for further details.

**Bit 4:** Inputs required from surface data are missing or in error. No retrieval is performed.

**Bit 5:** Inputs required from profile data are missing or in error. No retrieval is performed.

**Bit 6:** A retrieval was attempted and produced invalid values.

**Bit 7:** (Most significant bit) A retrieval was attempted and failed to converge.

**norm\_chi\_square** This is the chi square value calculated for the retrieved state, divided by the number of observations (see section 4.2). Values larger than 1 may be an indication of improper convergence.

**log\_N0, log\_N0\_uncert** The profile within the snow layer of the retrieved values of the  $\log_{10}$ -transformed intercept parameters of an assumed exponential snow particle size distribution (PSD), and their retrieved uncertainties.

**log\_lambda, log\_lambda\_uncert** The profile within the snow layer of the retrieved values of the  $\log_{10}$ -transformed slope parameters of an assumed exponential snow particle size distribution (PSD), and their retrieved uncertainties.

**snowfall\_rate, snowfall\_rate\_uncert** The profile within the snow layer of snowfall rates calculated using the retrieved values of  $\log_{10}(N_0)$  and  $\log_{10}(\lambda)$ , and the a priori model of snow microphysical properties. Uncertainties are calculated by propagating the retrieved uncertainties in  $\log_{10}(N_0)$  and  $\log_{10}(\lambda)$ , and the estimated a priori uncertainties in the snow microphysical property model into the snowfall rate calculation.

**snowfall\_rate\_sfc, snowfall\_rate\_sfc\_uncert** The estimated snowfall rate at the surface and its uncertainty. These are estimated as the snowfall rate and its uncertainty from the radar bin at the base of the snow layer.

**snowfall\_rate\_sfc\_confidence** Confidence in the surface snowfall rate for each profile represented by an integer value interpreted as follows:

**-1:** No retrieval or failed retrieval.

**0:** No confidence.

**1:** Very low confidence.

**2:** Low confidence.

**3:** Moderate confidence.

**4:** High confidence.

Values are set as shown in Table 2. For profiles which appear to have dry snow at the surface, the initial value is set to 3 (moderate confidence). If the surface type (2C-PRECIP-COLUMN variable Surface\_type) is other than “open ocean”, the value is reduced by 1. If the snowfall rate at the base of the truncated profile is substantially larger than that in the profile bin immediately above (bit 3 of retrieval\_status is set), the value is reduced by 1. Finally, the value is adjusted if multiple scattering and attenuation contribute substantial uncertainties to the modeled reflectivity at the base of the truncated profile. The adjusted value is limited to range between 0 (no confidence) and 4 (high confidence). For partially melted snow, the initial value is 1 (very low confidence), and no adjustments are applied.

Table 2: Settings for surface snowfall rate and its confidence value.

Surface Precip Type	melted mass fraction	snow layer/retrieval	Srate	confidence
Missing			missing	-1
None			0.	4
Rain			0.	4
Mixed	unknown		missing	-1
Mixed	(0.1, 1.0]		0.	1
Mixed	[0., 0.1]	absent/none	0.	0
“	“	present/failed	missing	-1
“	“	present/successful	per retrieval	1
“	“	unknown/none	missing	-1
Snow		absent/none	0.	0
“		present/failed	missing	-1
“		present/successful	per retrieval	3 + Mods
“		unknown/none	missing	-1

Table 3: Adjustments to the surface snowfall rate confidence value for forward model uncertainties due to multiple scattering and attenuation.

s(Ze), dBZe	Modifier
< 3	+1
3 - 6	0
6 - 12	-1
> 12	-2

#### **snow\_water\_content, snow\_water\_content\_uncert**

The profile within the snow layer of snow water contents calculated using the retrieved values of  $\log_{10}(N_0)$  and  $\log_{10}(\lambda)$ , and the a priori model of snow microphysical properties. Uncertainties are calculated by propagating the retrieved uncertainties in  $\log_{10}(N_0)$  and  $\log_{10}(\lambda)$ , and the estimated a priori uncertainties in the snow microphysical property model in the snow water content calculation.

#### **snow\_top\_height\_bin**

The index of the radar bin containing the snow echo top. The snow echo top is defined by the location at which, while traversing the snow layer from base to top, the observed reflectivity first drops below -15 dBZe. snow\_top\_height\_bin is the index of the bin immediately below this location, where the reflectivity is still above -15 dBZe.

## 2.2 Geolocation fields

All geolocation information is passed through from 2B-GEOPROF (Table 4). See documentation for the 2B-GEOPROF product for further details.

Table 4: 2C-SNOW-PROFILE geolocation fields.

Variable	Dimension	Units	Description
Profile_time	N <sub>ray</sub>	seconds	Seconds since the start of the granule for each profile
UTC_start	scalar	seconds	The UTC seconds since 00:00 UTC for the first profile in the granule
TAL_start	scalar	seconds	The International Atomic Time (seconds since 00:00:00 1 January 1993) for the first profile in the granule
Latitude	N <sub>ray</sub>	degrees	Spacecraft geodetic latitude
Longitude	N <sub>ray</sub>	degrees	Spacecraft geodetic longitude
Height	N <sub>bin</sub> , N <sub>ray</sub>	m	Height of radar range bins above mean sea level
DEM_elevation	N <sub>ray</sub>	m	Terrain elevation above mean sea level
Vertical_binsize	scalar	m	Effective vertical height of the radar range bins

## 3 Algorithm Theoretical Basis

Snowfall rate depends on the abundance of snow particles of different sizes (the particle size distribution, or PSD), the masses of those particles, and their fallspeeds. Fallspeeds in turn depend on particle masses, their shapes, and environmental conditions. As is true for lower-frequency precipitation radars, radar backscattering at the 94 GHz frequency used by the CPR is sensitive to PSD and particle masses; however, at this higher frequency, backscattering is also sensitive to particle shape. With even simple models for the PSD, the particle masses and the shapes, observations of 94 GHz radar reflectivity alone are insufficient to constrain the models sufficiently to determine snowfall rates. To address this insufficiency, optimal estimation is used as the retrieval method for 2C-SNOW-PROFILE. This method enables the use of explicit a priori information which can help constrain the retrievals. Additionally, optimal estimation allows uncertainties in the retrieval assumptions and observations to be propagated into estimates of uncertainties in retrieval products such as snowfall rate.

### 3.1 Radar reflectivity

At the frequencies used by cloud radars, scattering by precipitation-sized particles generally does not follow the Rayleigh approximation, and attenuation of the radar beam by hydrometeors and gases may be significant. Under these conditions and assuming single scattering, the effective radar reflectivity factor as a function of range from the radar is given by

$$Ze(R) = \frac{\Lambda^4}{\|K_w\|^2 \pi^5} \exp \left[ -2 \int_{s=0}^{s=R} \beta_{ext}(s) ds \right] \int_{D_{min}}^{D_{max}} N(D, R) \sigma_{bk}(D, R) dD \quad (1)$$

where  $R$  is the range,  $s$  is the position along the path of the beam,  $\sigma_{bk}(D, R)$  is the backscatter cross-section for particle size  $D$  at range  $R$ ,  $N(D, R)$  is the size distribution at range  $R$ ,  $\Lambda$  is the radar wavelength,  $\|K_w\|^2$  is the dielectric factor for water, and  $\beta_{ext}(s)$  is the volume extinction coefficient along the path of the radar beam. The exponential term is the two-way transmission between the radar and the observed radar volume at range  $R$  and represents losses in the transmitted and reflected power due to scattering and absorption along the path to the target.

The volume extinction coefficient includes contributions due to scattering and absorption by hydrometeors and due to absorption by gases, and is given by

$$\beta_{ext}(s) = \int_{D_{min}}^{D_{max}} N(D, s) \sigma_{ext}(D, s) dD + \sum_i k_{abs,i}(s) \rho_i(s) \quad (2)$$



where  $N(D, s)$  is the hydrometeor size distribution at position  $s$ ,  $\sigma_{ext}(D, s)$  is the hydrometeor extinction cross-section,  $k_{abs,i}(s)$  is the mass absorption coefficient for gas species  $i$ , and  $\rho_i(s)$  is the corresponding gas density. At 94 GHz, gaseous attenuation is predominantly due to water vapor; the two-way attenuation by water vapor in tropical atmospheres can approach 5 dB (Stephens et al., 2002). The 2B-GEOPROF product provides estimates of the two-way gaseous attenuation, and the snowfall retrieval algorithm uses these estimates to correct the 2B-GEOPROF reflectivities before a retrieval is performed.

Attenuation by frozen hydrometeors may also be substantial; however, under heavier snow conditions for which attenuation is a factor, multiple scattering partially offsets the attenuation (Matrosov and Battaglia, 2009). This compensating behavior in heavy snow causes the multiply-scattered attenuated reflectivity to lie between the singly-scattered nonattenuated and singly-scattered attenuated reflectivities. The results of Matrosov and Battaglia show that both the singly-scattered attenuated and nonattenuated reflectivities are biased estimates of the multiply-scattered attenuated reflectivity. Absent an explicit multiple scattering model for heavy snow, the multiply-scattered attenuated reflectivity may be approximated using the singly-scattered attenuated and nonattenuated reflectivities as bounding values. Additionally, the uncertainties for this approximation can be estimated from the difference in the singly-scattered attenuated and nonattenuated reflectivities.

Liquid hydrometeors also produce attenuation. While the CloudSat snowfall retrieval will not be applied to profiles thought to contain significant liquid cloud and rain, supercooled liquid water may also attenuate the radar beam. A single-wavelength, nadir-pointing radar such as the CPR lacks means for identifying the presence of supercooled water. Future developments may allow for treatment of attenuation by supercooled liquid water in the retrieval; for this product, this attenuation is omitted.

### 3.2 Snowfall rate

The snowfall rate  $S$  at some range  $R$  in the radar profile in units of liquid water depth per unit time is

$$S(R) = \frac{1}{\rho_{liq}} \int_{D_{min}}^{D_{max}} N(D, R) m(D, R) V(D, R) dD, \quad (3)$$

where  $m(D, R)$  is particle mass and  $V(D, R)$  is fallspeed, and  $\rho_{liq}$  is the density of liquid water. Fallspeeds may be described using explicit, physically-based relations. As described by Mitchell (1996), the dimensionless Best, or Davies, number  $X$  relates the Reynolds number  $Re$  and drag coefficient  $C_d$  for a falling particle and is expressed in terms of the particle mass and the particle area projected normal to the direction of motion:

$$X(D) = C_d Re^2 = \frac{2D^2 \rho_a g}{\mu^2} \frac{m(D)}{A_p(D)}, \quad (4)$$

where  $A_p(D)$  is the projected area of the particle,  $\rho_a$  is the air density,  $\mu$  is the viscosity, and  $g$  is gravitational acceleration. Arguments based on boundary layer theory for blunt bodies (Abraham, 1970) give an expression for  $Re$  in terms of the Best number, which Mitchell and Heymsfield (2005) modified to account for the enhancement of boundary layer effects in porous snow aggregates:

$$Re(D) = \frac{\delta_0^2}{4} \left[ \left( 1 + \frac{4\sqrt{X(D)}}{\delta_0^2 \sqrt{C_0}} \right)^{1/2} - 1 \right]^2 - a_0 [X(D)]^{b_0}, \quad (5)$$

with  $a_0 = 0.0017$  and  $b_0 = 0.8$  being parameters describing the enhanced boundary layer effects,  $\delta_0$  is a constant related to boundary layer thickness and  $C_0$  is the limiting drag coefficient under conditions dominated by pressure drag. Finally, the fallspeed can be found as

$$V(D) = \frac{Re(D) \mu}{\rho_a D}. \quad (6)$$

Note that  $D$  appears explicitly in the expressions for  $V(D)$  and  $X(D)$ , making them sensitive to the choice of  $D$ . For fallspeeds of nonspherical ice particles,  $D$  is taken typically to be the maximum dimension of the particle,  $D_M$ .

### 3.3 Particle model

The relationships described above require size-dependent particle properties including mass, horizontally-projected area, backscatter cross-sections, and extinction cross-sections. Particle masses and horizontally-projected areas are given by power laws (Locatelli and Hobbs, 1974; Mitchell, 1996)

$$m(D_M) = \alpha D_M^\beta \quad (7)$$

$$A_p(D_M) = \gamma D_M^\sigma. \quad (8)$$

For small particles, these relationships can produce masses which exceed those of ice spheres and areas which exceed those of circles, so for a given particle size  $D_M$ , particle mass is capped to be no greater than that of an ice sphere of the same diameter. Similarly, particle area is capped to be no more than that of a circle of the same diameter. Radar backscattering and extinction cross-sections are calculated via the discrete dipole approximation (Draine and Flatau, 1994), an approach suitable for irregularly-shaped particles.

Specifying the particle masses and areas partially constrain the dipole models needed to calculate scattering properties; however, additional assumptions must be made about particle shape. Additionally, the parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\sigma$  vary depending on factors including particle habit and degree of riming. The limited information available in reflectivity measurements precludes these properties from being retrieved. Instead, best estimates and uncertainties for the parameters and scattering properties were obtained from analyses of single particle measurement and other in-situ and remote sensing observations of snow particles (Wood, 2011). Dipole models were constructed using shapes found to best reproduce observed 94-GHz reflectivity measurements from a cold-season validation experiment (the Canadian CloudSat CALIPSO Validation Project, C3VP, (Hudak et al., 2006)). These a priori descriptions of particle properties constitute the particle model used by the algorithm.

### 3.4 Size distribution

Given the particle model, the remaining term needed to determine radar reflectivity or snowfall rate is the snow particle size distribution. Distributions of snow particle sizes are frequently characterized as exponential

$$N(D) = N_0 \exp(-\lambda D) \quad (9)$$

where  $\lambda$  is the slope of the distribution and  $N_0$  its intercept. While in general  $D$  may be either the melted drop diameter or an actual dimension of the particle, for 2C-SNOW-PROFILE an exponential form is used in which  $D$  is the maximum particle dimension,  $D_M$ .

Exponential behavior, especially at larger particle sizes, has been confirmed in aircraft-based in situ observations under a wide range of atmospheric conditions (Braham, 1990; Passarelli, 1978; Lo and Passarelli, 1982; Gordon and Marwitz, 1984; Houze et al., 1979; Woods et al., 2008). Some studies of aircraft observations have noted departures from exponential behavior (e.g., "super-" or "sub-exponential", Herzegh and Hobbs, 1985). Heymsfield et al. (2008) examined the adequacy of exponential distributions for snow, looking at the ability of a fitted exponential distribution to reproduce ice water contents and Rayleigh reflectivities calculated directly from the binned particle size distributions. They found that parameters derived from higher moments of the particle size distribution, which are more directly related to ice water content and radar reflectivity, produced exponential distributions which generally provided good agreement with IWC and Ze values calculated from the observed, binned size distributions.

For observations at the surface, estimates of size distributions based on actual particle dimension  $D_M$  have been far less common. Rogers (1973) used photographs of snowflakes to develop estimates of snow size distributions based on actual dimensions and also found snow size distributions to be exponential. Brandes et al. (2007) evaluated both exponential and gamma forms, which have the ability to represent sub- or super-exponential behavior, for snow size distributions observed by a 2D video disdrometer over the course of several winter seasons. Although about 22% of the observed snow distributions exhibited super-exponential features, more commonly the fitted gamma distributions were nearly equivalent to exponential distributions.

## 4 Implementation

A retrieval is performed for any profile which appears to contain snow and for which precipitation appears to be reaching the surface. If the precipitation reaching the surface is judged likely to be snow, the retrieval results are used to estimate the snowfall rate at the surface. For a given profile, the algorithm first performs a scene characterization then, if warranted, performs the retrieval and computes any derived quantities such as the surface snowfall rate.

### 4.1 Scene Characterization

Scene characterization determines if snow is present in the radar profile and if the snow is reaching the surface without significant melting. Because ground clutter contaminates the radar reflectivities in the range bins nearest the surface, these two evaluations are done independently.

#### 4.1.1 Near-surface bin

Before the profile is evaluated for the presence of snow, the clutter-contaminated range bins near the surface must be excluded. The number of excluded bins depends on the surface type. If the 2C-PRECIP-COLUMN variable `Surface_type` indicates the surface is ocean without sea ice, or inland water, the two range bins immediately above the surface-containing range bin are excluded. If the surface is identified as land, sea ice, or unknown, the four range bins immediately above the surface-containing range bin are excluded. This approach matches how 2C-PRECIP-COLUMN identifies the near-surface bin, the range bin that is nearest the surface and expected to be free of clutter.

#### 4.1.2 Profile characterization

Starting from the near-surface bin and working upward, the profile is examined for significant radar returns. Significant returns are those which have a 2B-GEOPROF `CPR_Cloud_mask` value greater than or equal to 20. Consistent with 2C-PRECIP-COLUMN, `CPR_Cloud_mask` values of 5 are also not excluded. If a significant return is present in the near-surface bin at the base of the profile, the lowest contiguous layer of significant returns is denoted as a hydrometeor layer.

The characteristics of this hydrometeor layer are then evaluated. First the reflectivity profile is examined to determine if precipitation is present using a reflectivity threshold of -15 dBZe. This threshold is based on the identification of very light liquid precipitation at -10 dBZe in Ka-band radar observations by Stephens and Wood (2007) and the “Rain possible” and “Snow possible” thresholds of Haynes et al. (2009). In the near-surface bin, the observed reflectivity is corrected for path integrated gaseous and hydrometeor attenuation, then compared to the threshold. Gaseous attenuation is obtained from the 2B-GEOPROF `Gaseous_attenuation` variable, and hydrometeor attenuation from the 2C-PRECIP-COLUMN `PIA_near_surface` variable. If the corrected reflectivity in the near-surface bin exceeds the threshold, precipitation is present and an upward search is made for the precipitation echo top. Since path integrated hydrometeor attenuation estimates are not available for range bins above the near-surface bin, the reflectivity profile above the near-surface bin is corrected only for gaseous attenuation. The precipitation echo top is identified as the first range bin for which the corrected reflectivity in the bin immediately above it falls below the -15 dBZe threshold. The contiguous layer from the near-surface bin to the precipitation echo top is identified as a precipitation layer. Starting from the precipitation echo top and working upward, the associated cloud echo top is then identified as the first range bin for which the reflectivity in the bin immediately above it falls below the minimum detectable signal of the radar.

Next, temperatures in the precipitation layer are examined to determine whether frozen precipitation is present. Using the ECMWF-AUX Temperature variable, if all temperatures are below 0° C, the entire precipitation layer is identified as snow. Otherwise, a search is made to find a contiguous frozen layer starting from the base of the precipitation layer. If such a layer is found, it is identified as snow. The top of this frozen precipitation is identified as the snow echo top. Finally, searching upward from the snow echo top to the associated cloud echo top, the scene characterization identifies the contiguous layer of frozen ( $T < 0^\circ \text{C}$ ) cloud-like radar bins

immediately above the snow echo top. These ice cloud bins together with the snow bins below the snow echo top make up the snow layer described initially in Section 1.

### 4.1.3 Surface precipitation characterization

An initial evaluation for snow at the surface is done using the 2C-PRECIP-COLUMN variables `Precip_flag` and `Melted_fraction`. If `Precip_flag` has a value of 4 (“snow possible”) or 5 (“snow certain”), 2C-SNOW-PROFILE indicates snow at the surface. If `Precip_flag` has a value of 6 (“mixed possible”) or 7 (“mixed certain”), the value of `Melted_fraction` is examined. If `Melted_fraction`  $\leq 0.1$ , 2C-SNOW-PROFILE also indicates snow at the surface. Otherwise, `Melted_fraction`  $> 0.1$ , or `Precip_flag` values of 1 (“rain possible”), 2 (“rain probable”) or 3 (“rain certain”) indicate precipitation reaching the surface. If the value of `Precip_flag` is missing, or if `Precip_flag` indicates mixed phase precipitation but `Melted_fraction` is missing, this state triggers a further attempt by the 2C-SNOW-PROFILE algorithm to evaluate the surface precipitation type.

If mixed phase precipitation is occurring but the melted fraction is unknown, the scene characterization will attempt to determine the melting depth (distance from the surface to the melting level) using the ECMWF-AUX temperature profile. If the melting depth is sufficiently shallow, the surface precipitation is considered to be snow. From the results of the melting layer model of Haynes et al. (2009), using a maximum allowed melting depth of 240 m (the height of a single vertical bin) gives a maximum melted mass fraction of about 0.15. With an assumed environmental lapse rate of  $6^\circ \text{ C km}^{-1}$ , this approach is equivalent to assuming snow exists at temperatures up to  $1.5^\circ \text{ C}$ . A similar threshold ( $2^\circ \text{ C}$ ) was found by Liu (2008) based on an analysis of present weather reports from shipboard and land station observations.

If the value of `Precip_flag` is missing, but the profile characterization identified a snow layer, the scene characterization will again attempt to determine the melting depth using the ECMWF-AUX temperature profile. If the melting depth is less than the threshold of 240 m, the surface precipitation is again considered to be snow.

## 4.2 Optimal estimation retrieval

The optimal estimation method for 2C-SNOW-PROFILE works by minimizing a cost function which represents differences between simulated and observed reflectivities and also differences between estimated and a priori values for the snow microphysical properties (Rodgers, 2000). Given a vector of reflectivity observations  $y$  and a state vector  $x$  of unknown microphysical properties to be retrieved, a corresponding reflectivity forward model  $F(x, \tilde{b})$  is constructed which relates  $x$  and  $y$ . The forward model may require other parameters,  $\tilde{b}$ , not to be retrieved, where the tilde indicates that these parameters may be known imperfectly. The forward model is typically an approximation of the true physical relation between  $x$  and  $y$ , and there are uncertainties associated with both the reflectivity observations  $y$  and the parameters  $\tilde{b}$ . Allowing for these uncertainties gives the statement of the forward problem:

$$y = F(x, \tilde{b}) + \varepsilon, \quad (10)$$

where  $\varepsilon$  represents the total uncertainty, due both to measurement uncertainty and to uncertainties in the forward model. These uncertainties may be due to both systematic and random errors.

It is desired to find the state  $\hat{x}$  which maximizes the posterior conditional probability density function (PDF)  $P(x | y)$ , subject also to prior knowledge about the values of  $x$ . This prior knowledge is described by expected values  $x_a$  and their covariances  $\mathbf{S}_a$ . The posterior PDF is evaluated by constructing the cost function

$$\Phi(x, y, x_a) = (y - F(x, \tilde{b}))^\top \mathbf{S}_\varepsilon^{-1} (y - F(x, \tilde{b})) + (x - x_a)^\top \mathbf{S}_a^{-1} (x - x_a), \quad (11)$$

and minimizing with respect to  $x$ , where  $\mathbf{S}_\varepsilon$  is the covariance matrix representing the uncertainties  $\varepsilon$ . If  $\varepsilon$  contains systematic errors which can be identified, it is desirable to correct for them by adjusting the model or measurements and determining a corrected  $\mathbf{S}_\varepsilon$  (Marks and Rodger, 1993).

Provided the forward model is not excessively nonlinear, the vector  $\hat{x}$  which minimizes the cost function can be found by Newtonian iteration:

$$\hat{x}_{i+1} = \hat{x}_i + \left( \mathbf{S}_a^{-1} + \mathbf{K}_i^\top \mathbf{S}_\varepsilon^{-1} \mathbf{K}_i \right)^{-1} \left[ \mathbf{K}_i^\top \mathbf{S}_\varepsilon^{-1} (y - F(\hat{x}_i, \tilde{b})) - \mathbf{S}_a^{-1} (\hat{x}_i - x_a) \right], \quad (12)$$

where  $\mathbf{K}$  is the Jacobian of the forward model with respect to the state vector, and  $\mathbf{K}_i = \mathbf{K}(\hat{x}_i)$ . Iteration continues until the covariance-weighted difference in successive state vector estimates is much smaller than the number of state vector elements. At convergence, the covariance of the solution  $\hat{x}$  is obtained as

$$\hat{\mathbf{S}}_x = \left( \hat{\mathbf{K}}^\top \mathbf{S}_\varepsilon^{-1} \hat{\mathbf{K}} + \mathbf{S}_a^{-1} \right)^{-1}, \quad (13)$$

where  $\hat{\mathbf{K}} = \mathbf{K}(\hat{x})$ . As a diagnostic test of the results, a  $\chi^2$  statistic is calculated using the retrieved state vector in (11). A value near  $N_y$ , the number of observations, suggests correct convergence.

The observation vector for this retrieval is the vertical profile of reflectivities observed by CloudSat, corrected for gaseous attenuation,

$$y = \begin{bmatrix} Ze_1 \\ \vdots \\ Ze_{N_y} \end{bmatrix} \quad (14)$$

where  $N_y$  is the number of radar range bins in the snow layer. Because of the large range of  $Ze$ , the values used for the retrieval are in decibels.

The state at each radar bin is described by the exponential size distribution parameters  $N_0$  and  $\lambda$ . Values for  $N_0$  may range over several orders of magnitude, so  $\log(N_0)$  is retrieved instead. The variability of  $\lambda$  is significantly smaller than that of  $N_0$ ; however, examination of fitted exponential distributions from C3VP snow events showed that the distribution of values for  $\lambda$  was strongly non-Gaussian. The log-transformed values are much less skewed, and accordingly,  $\log(\lambda)$  is retrieved instead. The corresponding state vector to be retrieved is then

$$\hat{x} = \begin{bmatrix} \log(N_0)_1 \\ \vdots \\ \log(N_0)_{N_y} \\ \log(\lambda)_1 \\ \vdots \\ \log(\lambda)_{N_y} \end{bmatrix}. \quad (15)$$

and the associated covariance matrix is

$$\hat{\mathbf{S}}_x = \begin{bmatrix} s^2(\log(N_0)_1) & \dots & \dots & s(\log(N_0)_1, \log(\lambda)_{N_y}) \\ \vdots & \ddots & \vdots & \vdots \\ \vdots & s^2(\log(N_0)_{N_y}) & \vdots & \vdots \\ \vdots & \vdots & s^2(\log(\lambda)_1) & \vdots \\ \vdots & \vdots & \vdots & \ddots \\ s(\log(N_0)_1, \log(\lambda)_{N_y}) & \dots & \dots & s^2(\log(\lambda)_{N_y}) \end{bmatrix}. \quad (16)$$

#### 4.2.1 Radar forward model

Following the reasoning described in the discussion of multiple scattering and attenuation, both the singly-scattered attenuated and nonattenuated reflectivities are modeled. Applying the exponential distribution with (1) and omitting the attenuation term, the singly-scattered nonattenuated reflectivity  $Ze^{ss,na}$  at range bin  $i$  is

$$Ze^{ss,na}(N_{0,i}; \lambda_i; \tilde{b}_i) = \frac{\Lambda^4}{\|\mathbf{K}_w\|^2 \pi^5} \int_{D_{M,min}}^{D_{M,max}} N_{0,i} \exp(-\lambda_i D_M) \sigma_{bk}(D_M, \tilde{b}_i) dD_M. \quad (17)$$

The backscatter cross-section  $\sigma_{bk}$  has been written to show its dependence on a vector of parameters  $\tilde{\mathbf{b}}_i$  as well as on  $D_M$ . The vector  $\tilde{\mathbf{b}}_i$  includes the parameters for the mass- and area-dimension relations  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\sigma$  which were used to construct the particle models from which the scattering properties were calculated. The tilde indicates that these parameters are approximations of the true values. Following (1) and (2), the singly-scattered attenuated reflectivity  $Ze^{ss,a}$  is

$$Ze^{ss,a}(N_{0,i}; \lambda_i; \tilde{\mathbf{b}}_i; R_i) = Ze^{ss,na}(N_{0,i}; \lambda_i; \tilde{\mathbf{b}}_i) (\mathcal{T}(R_{0,i}))^2 \quad (18)$$

where  $R_{0,i}$  is the range to bin  $i$  and  $\mathcal{T}$  is the one-way transmission to the radar bin:

$$\mathcal{T}(R_{0,i}) = \mathcal{T}_{0,i} = \exp \left[ - \int_{s=0}^{s=R_{0,i}} \beta_{ext}(s) ds \right]. \quad (19)$$

Since reflectivities have been corrected for gaseous attenuation, the volume extinction coefficient  $\beta_{ext}$  is

$$\beta_{ext}(s) = \int_{D_{M,min}}^{D_{M,max}} N_0(s) \exp(-\lambda(s)D_M) \sigma_{ext}(D_M, \tilde{\mathbf{b}}(s)) dD_M. \quad (20)$$

The dependence of  $\mathcal{T}$  on the vertical profile of  $N_0$  and  $\lambda$  has been omitted from the notation for clarity.

The results of Matrosov and Battaglia (2009) shown in their Figure 3 suggest that the multiply-scattered attenuated reflectivity  $Ze^{ma,a}$  falls approximately midway between  $Ze^{ss,a}$  and  $Ze^{ss,na}$  in decibel units. Accordingly  $Ze^{ms,a}$  at radar bin  $i$  is approximated as the geometric mean of the two singly-scattered reflectivities in linear units,

$$\begin{aligned} Ze_i^{ms,a} &\approx [Ze_i^{ss,na} Ze_i^{ss,a}]^{1/2} \\ &\approx Ze_i^{ss,na} \mathcal{T}_{0,i}. \end{aligned} \quad (21)$$

The vector  $F$  of forward modeled reflectivities is then

$$F = \begin{bmatrix} dBZe_1^{ms,a} \\ \vdots \\ dBZe_{N_y}^{ms,a} \end{bmatrix} = \begin{bmatrix} Ze_1^{ss,na} \mathcal{T}_{0,1} \\ \vdots \\ Ze_{N_y}^{ss,na} \mathcal{T}_{0,N_y} \end{bmatrix} \quad (22)$$

or, in decibel units,

$$F = \begin{bmatrix} dBZe_1^{ss,na} + dB\mathcal{T}_{0,1} \\ \vdots \\ dBZe_{N_y}^{ss,na} + dB\mathcal{T}_{0,N_y} \end{bmatrix} \quad (23)$$

where  $dB\mathcal{T}_{0,i} = 10 \log(\mathcal{T}_{0,i})$ . This approach amounts to an estimated bias correction applied to the singly-scattered nonattenuated reflectivities  $dBZe_i^{ss,na}$ .

#### 4.2.2 Measurement and forward model uncertainties

The error covariance matrix  $\mathbf{S}_\epsilon$  describes the uncertainties associated with model-measurement differences for the CloudSat retrieval and is composed of two terms:

$$\mathbf{S}_\epsilon = \mathbf{S}_y + \mathbf{S}_F \quad (24)$$

where  $\mathbf{S}_y$  is the covariance matrix describing the measurement uncertainties and  $\mathbf{S}_F$  is the forward model error covariance matrix.

The sources of measurement uncertainty include uncertainty in the absolute radiometric calibration and measurement noise. The noise characteristics of the CPR vary with signal strength. For reflectivities above -10 dBZ, one standard deviation of noise as a fraction of the mean signal is about -16 dB, while for reflectivities below -10 dBZ, noise is an increasing fraction of the signal, reaching 0 dB at the minimum detectable signal of

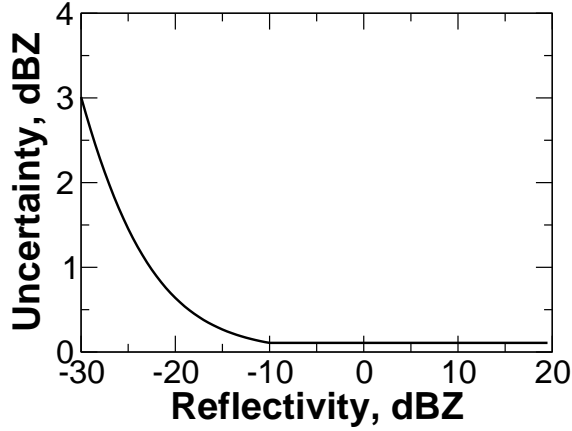


Figure 1: Upward uncertainty based on one standard deviation of noise for the CloudSat CPR.

-30 dBZ (R. Austin, personal communication, 4 November, 2008). The resulting uncertainties range from 3 dBZ for a reflectivity of -30 dBZ to about 0.1 dBZ for reflectivities above -10 dBZe. (Figure 1). Calibration errors, which would result in a bias in the measured reflectivities, are expected to be less than 2 dB based on a prelaunch calibration error budget (Tanelli et al., 2008), but the value of this bias is unknown and isn't considered. To construct  $\mathbf{S}_y$ , variances for each range bin are computed as the squares of these uncertainties and uncertainties in distinct range bins are considered to be uncorrelated, resulting in a diagonal form for  $\mathbf{S}_y$ .

Several sources contribute to the forward model uncertainties represented by  $\mathbf{S}_F$ . A complete description of the methods used to assess these sources and the resulting uncertainties can be found in (Wood, 2011). Briefly, the forward-modeled reflectivities have uncertainties due to two sources: first, the approximate nature of the transmission-based bias correction for multiple scattering and attenuation given in (21); and second, the uncertainties in the singly-scattered nonattenuated reflectivities given in (17). For the first source, the values of  $Ze^{ss,na}$  and  $Ze^{ss,a}$  place upper and lower bounds on the expected value of  $Ze^{ms,a}$  and can be used to make a rudimentary estimate of this uncertainty. The estimate used here is that the uncertainty in  $Ze^{ms,a}$  is one-half the difference between  $Ze^{ms,a}$  and  $Ze^{ss,na}$  in decibels. The resulting estimate of the variance at each radar bin is then

$$\begin{aligned} s^2(dBZe_i^{ms,a}) &= \left[ \frac{1}{2} (dBZe_i^{ss,na} - dBZe_i^{ms,a}) \right]^2 \\ &= \left[ \frac{1}{2} dB\mathcal{T}_{0,i} \right]^2. \end{aligned} \quad (25)$$

This simple approach is not sufficient to diagnose vertical correlations in these uncertainties, so covariances between radar bins are set to zero so that the resulting covariance matrix is diagonal.

For the second source, the uncertainties may be further decomposed as the sum of two terms:  $\mathbf{S}_B^{ss,na}$ , which is a covariance matrix describing uncertainties due to the forward model parameters  $\tilde{\mathbf{b}}$ , and  $\mathbf{S}_F^{ss,na}$ , which is a covariance matrix describing uncertainties due to other assumptions in the calculation of  $Ze^{ss,na}$ .  $\mathbf{S}_B^{ss,na}$  is calculated as

$$\mathbf{S}_B^{ss,na} = \mathbf{K}_b \mathbf{S}_b \mathbf{K}_b^T \quad (26)$$

where  $\mathbf{K}_b$  is the Jacobian of the forward model reflectivities with respect to the parameters  $\tilde{\mathbf{b}}$  and  $\mathbf{S}_b$  is the covariance matrix for the parameters. Per (17),  $\tilde{\mathbf{b}}$  includes the microphysical parameters  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\sigma$  used to construct the particle models and calculate scattering properties.  $\mathbf{K}_b$  depends on the estimated state  $\hat{\mathbf{x}}$  and so is evaluated at each iterative step using a set of perturbed particle models. In general,  $\mathbf{S}_B^{ss,na}$  is not diagonal, because attenuation causes reflectivities in the profile to be dependent on the state of radar bins at higher altitudes and so  $\mathbf{K}_b$  is not diagonal.

The forward modeled reflectivities depend on other assumptions whose contributions to uncertainties are quantified in  $\mathbf{S}_F^{ss,na}$ . These sources include the choice of particle shape, the placement of dipoles in the DDA

models, discretization and truncation of the integrations over size distribution, and the assumption of the exponential distribution. Analyses using alternate DDA dipole models and observed particle size distributions provided estimates for these terms, which are expected to be uncorrelated with each other and with uncertainties in adjacent radar bins, giving  $\mathbf{S}_F^{ss,na}$  diagonal form.

#### 4.2.3 A priori estimates of the state

For each profile, the a priori state consists of a vector of expected values  $x_a$  and the corresponding covariance matrix  $\mathbf{S}_a$ , having the same sizes as the state vector  $x$  (15) and its covariance matrix  $\mathbf{S}_x$  (16). A priori estimates of  $\log(N_0)$  and  $\log(\lambda)$  at each bin of the snow layer are determined using temperature-based parameterizations derived from snow PSDs observed during C3VP and in conjunction with PSDs from other field experiments (Wood, 2011). Values vary through the profile depending on the temperatures in the ECMWF-AUX product. Uncertainties in the values arise because of natural variability and errors in the observations, and were estimated using the residual standard deviations between the parameterized and observed values. The uncertainty model also includes covariance between  $\log(N_0)$  and  $\log(\lambda)$  within each radar bin, as indicated by the analyzed observations, giving  $\mathbf{S}_a$  a tridiagonal form. For the retrieval iterations, the a priori covariance matrix is scaled to larger values to allow the a priori state to stabilize the retrieval without causing bias. The unscaled covariance matrix is then used to estimate the uncertainties in the retrieved state.

### 4.3 Derived products: Snowfall rate and snow water content

Provided a retrieval is successful, snowfall rates are calculated as described in Section 3.2 from the retrieval results for each radar bin in the snow layer. Uncertainties for snowfall rate are determined in a manner similar to that used for the forward model uncertainties. The total uncertainty is decomposed into terms due to 1) uncertainties in the retrieved state, 2) uncertainties in the particle model parameters, 3) uncertainties in the fallspeed model, and 4) uncertainties associated with the assumed exponential distribution. These terms are evaluated using the covariance matrix for the retrieved state,  $\hat{\mathbf{S}}_x$  as well as the results from several other analyses as described in Wood (2011). Snow water contents are calculated analogously as

$$SWC(R) = \int_{D_{min}}^{D_{max}} N(D, R) m(D, R) dD, \quad (27)$$

along with uncertainties. The surface snowfall rate and its uncertainty are taken to be equal to the values at the base of the snow layer.

## 5 Algorithm Inputs

The algorithm uses inputs from the 1B-CPR, 2B-GEOPROF, 2C-PRECIP-COLUMN and ECMWF-AUX products (Table 5).



Table 5: 2C-SNOW-PROFILE inputs.

Source	Name	Dimension	Units
1B-CPR	RayHeader_RangeBinSize	scalar	m
2B-GEOPROF	TAL_start	scalar	seconds
“	Latitude	$N_{ray}$	degrees
“	Longitude	$N_{ray}$	degrees
“	Height	$N_{bin}, N_{ray}$	m
“	DEM_elevation	$N_{ray}$	m
“	Vertical_binsize	scalar	m
“	SurfaceHeightBin	$N_{ray}$	–
“	CPR_Cloud_mask	$N_{bin}, N_{ray}$	–
“	Gaseous_Attenuation	$N_{bin}, N_{ray}$	dB
“	Radar_Reflectivity	$N_{bin}, N_{ray}$	dBZe
“	sem_MDSignal	$N_{ray}$	dBZe
2C-PRECIP-COLUMN	Precip_flag	$N_{ray}$	–
“	Melted_fraction	$N_{ray}$	–
“	Surface_type	$N_{ray}$	–
“	PIA_near_surface	$N_{ray}$	dB
ECMWF-AUX	Temperature	$N_{bin}, N_{ray}$	K
“	Pressure	$N_{bin}, N_{ray}$	Pa

## 6 Output file data structure

Table 6 summarizes the output file data structure.

Table 6: 2C-SNOW-PROFILE output file data structure

Data Granule	Swath Data		Variable Name	Dimension	Units
	Swath Data	Geolocation Fields	Profile_time	$N_{\text{ray}}$	seconds
			UTC_start	scalar	seconds
			TAL_start	scalar	seconds
			Latitude	$N_{\text{ray}}$	degrees
			Longitude	$N_{\text{ray}}$	degrees
			Height	$N_{\text{ray}}$	m
			DEM_elevation	$N_{\text{ray}}$	m
			Vertical_binsize	scalar	m
		2B-GEOPROF pass-through fields	Data_quality	$N_{\text{ray}}$	–
			Data_status	$N_{\text{ray}}$	–
			Data_targetID	$N_{\text{ray}}$	–
		2C-SNOW-PROFILE data fields	snow_retrieval_status	$N_{\text{ray}}$	–
			norm_chi_square	$N_{\text{ray}}$	–
			snowfall_rate	$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$
	snowfall_rate_uncert		$N_{\text{bin}}, N_{\text{ray}}$	$\text{mm h}^{-1}$	
	log_N0		$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{m}^{-3}\text{mm}^{-1})$	
	log_N0_uncert		$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{m}^{-3}\text{mm}^{-1})$	
	log_lambda		$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{mm}^{-1})$	
	log_lambda_uncert		$N_{\text{bin}}, N_{\text{ray}}$	$\log_{10}(\text{mm}^{-1})$	
	snowfall_rate_sfc		$N_{\text{ray}}$	$\text{mm h}^{-1}$	
	snowfall_rate_sfc_uncert		$N_{\text{ray}}$	$\text{mm h}^{-1}$	
	snowfall_rate_sfc_confidence		$N_{\text{ray}}$	–	
	snow_water_content		$N_{\text{bin}}, N_{\text{ray}}$	$\text{g m}^{-3}$	
	snow_water_content_uncert		$N_{\text{bin}}, N_{\text{ray}}$	$\text{g m}^{-3}$	
	snow_echo_top_bin	$N_{\text{ray}}$	–		

## 7 Retrieval Examples

Figure 2 provides an example of a snowfall scene from granule 3451 and the corresponding retrieval results. Over land surfaces such as this, the near-surface bin is placed at the 5th bin above the bin containing the surface. For some profiles in the southern portion of this scene, although significant reflectivity is present in the near-surface bin, the reflectivity does not meet the precipitation threshold and no retrieval is performed. For profiles in the northern portion of the scene, the near-surface bin does not contain significant reflectivities.

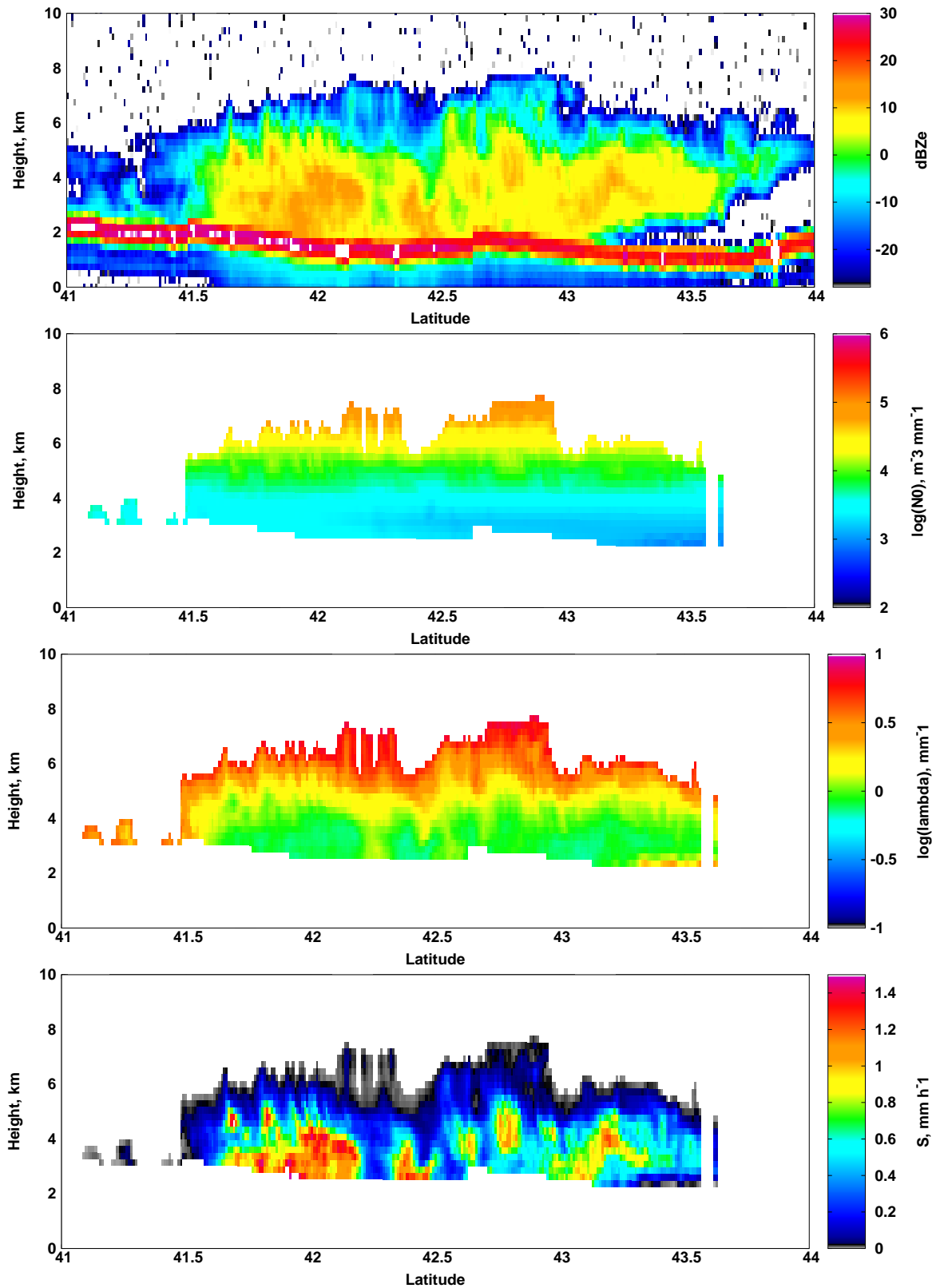


Figure 2: Retrieval example from granule 3451, showing (from top to bottom) the reflectivity field from 2B-GEOPROF, the retrieved values of  $\log(N_0)$  and  $\log(\lambda)$ , and the resulting snowfall rates calculated from the retrieved values.

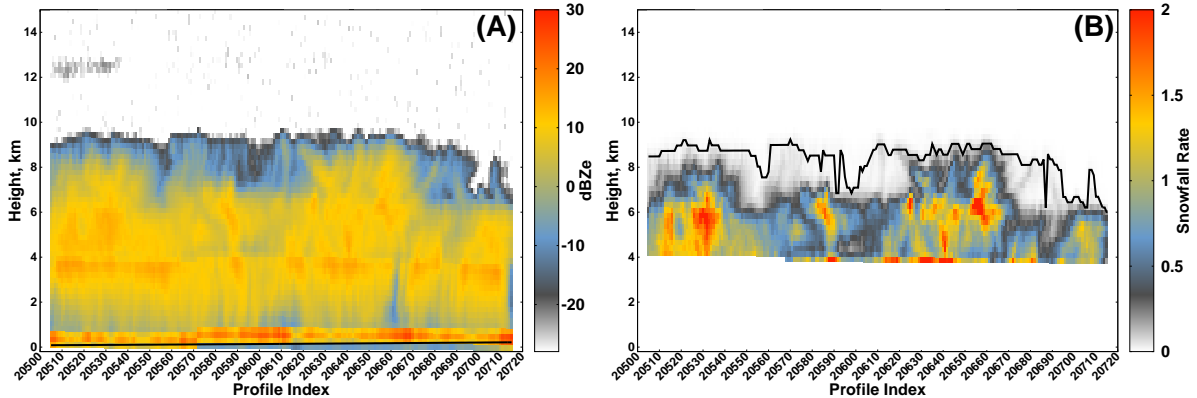


Figure 3: Illustration of major modifications for the P1\_R05 version of 2C-SNOW-PROFILE, from granule 08478. (A) reflectivity profiles, showing the melting level. (B) Retrieved estimates of snowfall rate above the melting level with the snow echo top indicated by the heavy black line.

Figure 3 illustrates the case of a snowfall retrieval above the melting level when rain or mixed-phase melted precipitation is reaching the surface. On the left (panel A), the reflectivity profiles show enhanced reflectivities at the melting level just below 4 km. The right panel (B) shows the retrieval estimates of snowfall rates. The heavy black line indicates the location of the snow echo top at  $-15$  dBZe. Note the weak retrievals in the cloud-like regions above the snow echo top and the instances of larger snowfall rates at the base of the retrieved layer. These snowfall rate estimates are a result of the larger reflectivities due to snow melt at the very top of the melting level. Users of these data for snow properties above the melting level should refer to section 8 for relevant cautions.

## 8 Caveats and Known Issues

**Retrieval status bit 3** Bit 3 of `snow_retrieval_status` is set when the snowfall rate in the near-surface bin is substantially different from that in the bin immediately above. This situation may arise in several different scenarios. First, for steeply-varying terrain, it is presently unclear whether placing the near-surface bin in the 5th bin above the surface is sufficient to eliminate the effects of ground clutter on retrievals for snow scenes. Ground clutter effects in this bin have the potential to cause the retrieval to produce anomalously high snowfall rates which would likely not be present in the bin above. Second, partial melting of snow particles may enhance radar reflectivity. The forward model used by the retrieval assumes dry snow properties. To reproduce the enhanced reflectivity, the retrieval would likely overestimate snowfall rate in the bin containing the melted particles. Finally, shallow precipitation might lead to a significant snowfall rate in the near-surface bin with none in the bin above.

Two separate criteria are used to set bit 3. First, in scenes for which the near-surface bin is the only bin in the snow layer, bit 3 is set if the snowfall rate in the near-surface bin exceeds  $5 \text{ mm h}^{-1}$ . This threshold was determined based on an evaluation of the distribution of retrieved snowfall rates under this scenario, which showed a bimodal distribution with a minimum at approximately  $5 \text{ mm h}^{-1}$ . Second, if the near-surface bin and the bin immediately above both contain snow, bit 3 is set if the ratio of the snowfall rate in the lower bin to that in the upper bin exceeds a threshold based on the snowfall rate in the upper bin. This threshold was determined by comparing distributions of these ratios with distributions of corresponding ratios from bins slightly higher in the retrieved profiles.

Users should evaluate whether the flagged profiles are of concern for their analyses. In situations where the users conclude the flagged profiles may be affected by ground clutter, retrieval results for the bin above the near-surface bin may be used to estimate the surface snowfall rate; however, since each retrieval is performed on the snow layer as a whole, the results in distinct bins are not fully independent.

**Fallspeeds** The fallspeeds for snow particles, used to calculate snowfall rates from the retrieval results, are calculated using a parameterization for particle terminal velocities (Mitchell and Heymsfield, 2005). Fallspeeds

are assumed to equal the terminal velocities; however, this assumption is accurate only for environments with no vertical air motion. In convective scenes, in particular, fallspeeds may depart significantly from the calculated terminal velocities. At present the algorithm does not have a method for identifying profiles for which the fallspeed assumption is likely significantly violated.

**Partial melting aloft** Users should keep in mind that the location of the melting layer is determined from the temperature profile provided from the ECMWF-AUX product and that location may not precisely coincide with the radar reflectivity profiles. As a result, snow properties near the base of the snow layer may be influenced by enhanced reflectivities that result as snow particles begin to melt. Users interested in using these retrievals of snow properties above the melting layer should apply caution and consider whether further processing of the data is needed to exclude retrieval results influenced by partial melting.

## 9 Operator Instructions

The 2C-SNOW-PROFILE algorithm operates as part of the CloudSat Operational and Research Environment (CORE). For each processed granule, the algorithm produces a metadata file at the conclusion of processing. The metadata contains counts of the number of profiles classified as having snow or predominantly frozen mixed-phase precipitation at the surface, along with counts profiles with failed retrievals or with data insufficient for the retrieval to run. Additionally, the metadata contains a histogram of surface snowfall rates.

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# Appendices

## Particle model

Values for the parameters of the mass- and area-dimension power functions are

$$\begin{aligned}\ln(\alpha) &= -5.723 \\ \beta &= 2.248 \\ \ln(\gamma) &= -1.379 \\ \sigma &= 1.813\end{aligned}$$

with error covariance matrix

$$\mathbf{S}_b = \begin{pmatrix} 0.592 & 0.212 & 0.090 & 0.023 \\ 0.212 & 0.142 & 0.011 & 0.007 \\ 0.090 & 0.011 & 0.335 & 0.103 \\ 0.023 & 0.007 & 0.103 & 0.046 \end{pmatrix}.$$

These values are appropriate for use with particle size  $D_M$  in centimeters. The radar backscatter and extinction cross-sections are given below (Table 7) as functions of particle size.

## Evaluating snow\_retrieval\_status

The output variable `snow_retrieval_status` contains 8-bit values where for each value, sometimes called a bitfield, the state of individual bits signal particular characteristics of the profile, its scene characterization and its retrieval results (section 2.1). This example shows an element with bit positions 3, 1, and 0 set (following convention, bit positions are numbered here from 7 at the left to 0 at the right).

```
bit value: 00001011
bit position: 76543210
```

Note that this bitfield is also the binary representation of the decimal integer value 11, a fact used in the example code below.

Software languages generally provide means for testing whether or not the bit in a particular position is set. This series of Fortran statements serve to test whether bit 3 is set using the Fortran function `btest()`. In `snow_retrieval_status`, bit 3 is used to indicate a large vertical gradient in snowfall rate at the near-surface bin.

```
integer(kind=1) :: status_value      !This is an element from snow_retrieval_status
integer :: bit_position
logical :: bit_set

status_value = 11 !Decimal integer equivalent to '00001011'

bit_position = 3
bit_set = btest(status_value, bit_position)

if (bit_set) then
  print *, "Large vertical gradient in snowfall rate at near-surface bin"
end if
```

In Python, `snow_retrieval_status` values can be saved in a NumPy array of type `numpy.uint8`, and the utility `numpy.unpackbits()` can extract the corresponding array of bit values. Results similar to the above would be achieved as follows:



```
import numpy
snow_retrieval_status = numpy.zeros((1,), dtype=numpy.uint8)
snow_retrieval_status[0] = 0b0001011
bitfield = numpy.unpackbits(snow_retrieval_status[0])
#Note that numpy.unpackbits() returns an 8-element array of bits,
#but index 7 is the rightmost bit and index 0 is the leftmost bit,
#so reverse the bitfield
bitfield = bitfield[::-1]

bit_position = 3
if bitfield[bit_position]:
    print "Large vertical gradient in snowfall rate at near-surface bin"
```

Table 7: Particle scattering cross-sections

$D_M$ mm	$C_{bk}$ m <sup>2</sup>	$C_{ext}$ m <sup>2</sup>
0.025	5.16253e-17	3.52024e-14
0.050	1.20475e-15	1.77890e-13
0.075	8.27182e-15	5.00664e-13
0.100	3.06847e-14	9.89618e-13
0.125	8.40498e-14	1.67138e-12
0.150	1.92314e-13	2.58903e-12
0.200	7.17250e-13	5.30976e-12
0.250	1.91396e-12	9.14038e-12
0.300	4.35436e-12	1.48681e-11
0.350	8.56280e-12	2.25304e-11
0.400	1.54761e-11	3.31046e-11
0.450	2.58963e-11	4.69409e-11
0.500	4.11161e-11	6.52071e-11
0.600	8.93929e-11	1.16523e-10
0.700	1.75650e-10	2.00793e-10
0.800	3.06043e-10	3.20526e-10
0.900	4.97542e-10	4.93081e-10
1.000	7.65231e-10	7.27755e-10
1.250	1.82454e-09	1.67311e-09
1.500	3.56830e-09	3.30096e-09
1.750	5.83188e-09	5.75812e-09
2.000	8.34684e-09	9.01675e-09
2.250	1.10293e-08	1.33794e-08
2.500	1.38623e-08	1.90102e-08
2.750	1.50482e-08	2.53761e-08
3.000	1.60708e-08	3.31323e-08
3.250	1.64139e-08	4.21088e-08
3.500	1.66119e-08	5.22600e-08
4.000	1.55864e-08	7.74061e-08
4.500	1.77554e-08	1.11609e-07
5.000	3.06798e-08	1.58860e-07
5.500	1.93705e-08	2.00667e-07
6.000	1.04092e-07	2.83080e-07
6.500	9.75512e-08	3.35067e-07
7.000	1.49787e-07	4.13047e-07
7.500	2.30734e-07	5.10512e-07
8.000	3.13418e-07	6.07034e-07
8.500	2.88081e-07	7.06213e-07
9.000	2.94080e-07	8.59293e-07
9.500	2.01596e-07	9.74101e-07
10.000	2.07686e-07	1.12076e-06
11.000	2.33291e-07	1.46061e-06
12.000	5.94999e-07	1.90676e-06
13.000	5.45403e-07	2.27318e-06
14.000	6.63279e-07	2.81244e-06
15.000	9.90939e-07	3.58772e-06
16.000	6.39329e-07	4.18269e-06
17.000	7.07551e-07	4.86569e-06
18.000	1.05353e-06	5.83543e-06