

CloudSat Project

A NASA Earth System Science Pathfinder Mission

## **Level 2 Cloud Optical Depth Product Process Description and Interface Control Document**

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## 1 Introduction

This document provides an overview of the 2B-TAU cloud optical depth retrieval algorithm. The document describes the algorithm's:

- purpose,
- scientific basis,
- required inputs,
- implementation,
- outputs, and
- operator instructions.

### 1.1 Purpose

The primary objective of the algorithm is to produce estimates of the optical depth ( $\tau$ ) and its uncertainty for each radar profile determined to contain cloud. However, as shown below, to obtain accurate estimates of optical depth,  $\tau$ , the effective radius,  $r_{eff}$ , must be retrieved as well (Breon et al.[1]). To appreciate the importance of retrieving  $r_{eff}$ , Fig. 1a and 1b illustrate the consequences of assuming an incorrect asymmetry factor on the retrieved optical depth.

MODIS reflectivities depend upon the observational geometry (observational,  $\theta$ , and solar zenith,  $\theta_0$ , angles, azimuthal angle difference,  $\phi - \phi_0$ ) according to the geographical position of AQUA satellite. Although these angles range from nadir to about  $20^\circ$ , retrievals performed at nadir would be calculated at higher speed, but would incur intolerably large errors as shown in Fig 1c. The selected algorithm allows for arbitrary viewing angles. The optical depth and effective radius are retrieved using upwelling reflectivity at the top of the atmosphere (TOA) measured by MODIS in several channels and other ancillary data (e.g., geolocation, meteorological parameters and surface albedo). The retrieved values are spectral and represent the optical depth and effective radius at the short wave. The radar reflectivity measured by the CloudSat Profiling Radar (CPR) provides information about the cloud distribution in the atmospheric column, and serves as a quantitative basis to produce cloud optical depth profiles.

## 2 Basis of the Algorithm

### 2.1 Overview

The retrieval uses a Bayesian statistical approach described by Marks and Rogers [2]. The retrieved state vector containing the optical depth and effective radius is obtained by using the MODIS reflectivity measurements to refine *a priori* information and also subjects to the uncertainties in both the *a priori* information and the measurement uncertainties. The CPR reflectivity is used to produce the *a priori* value of  $\tau$  and its associated uncertainty. Another fundamental component is a forward model which provides us with the simulated TOA reflectivities for the atmospheric model described by the state vector. Comparison between the simulated and measured TOA reflectivities is used to update the state vector and

allows us to converge iteratively to a solution. The forward model uses a multi-stream plane-parallel adding model (Christi and Gabriel [3]) based on methods by Benedetti et al. [4]. The next subsection contains a brief description of the retrieval algorithm components.

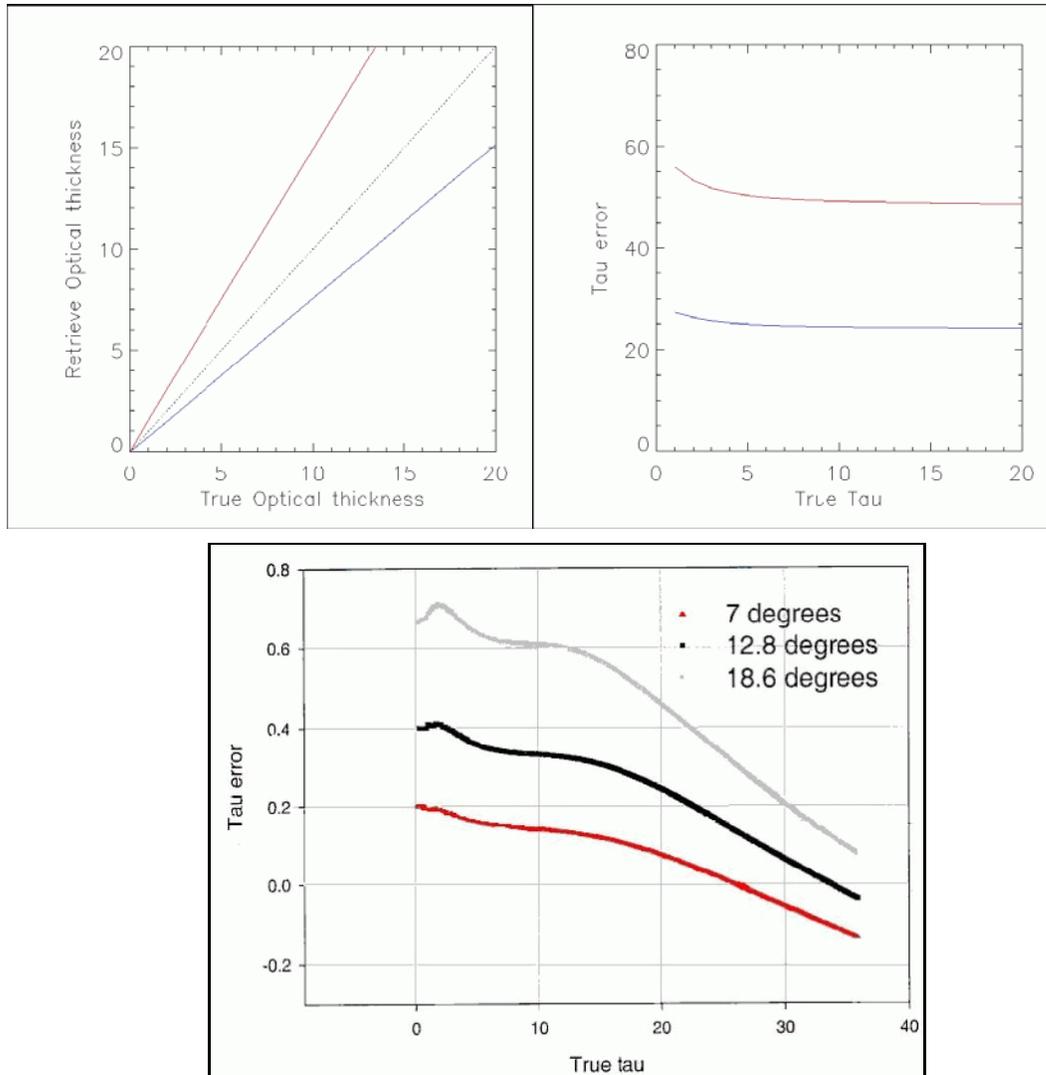


Fig. 1: a) Retrieved optical depth for different asymmetry factors (colored lines). True asymmetry factor is  $g=0.85$ . b) As in a) except that errors are shown. c) Error on retrieved optical depth due to incorrect observation angle. True exiting reflectivities at indicated angles are shown by colored lines. Retrieved optical depths computed at Nadir

## 2.2 Forward Radiative Transfer Model

### 2.2.1 Theory

The model used here incorporates a cloud layer overlying a reflecting surface. The optical properties of the cloud and surface are assumed to be horizontally homogeneous. In addition, the optical

properties of the cloud are assumed to be vertically homogeneous. Given these assumptions the monochromatic 1D radiative transfer equation (RTE):

$$\mu \frac{dI(\tau, \mu, \phi)}{d\tau} = -I(\tau, \mu, \phi) + \frac{\omega}{4\pi} \int_0^1 \int_{-1}^1 P(\mu, \phi; \mu', \phi') I(\tau, \mu', \phi') d\mu' d\phi' + S(\tau, \mu, \phi), \quad (2.1)$$

where  $I(\tau, \mu, \phi)$  is the radiance observed at a height expressed by the optical depth  $\tau$  in the direction given by  $\mu = \cos(\theta)$  and  $\phi$ ,  $\omega$  is the single scattering albedo, which is measure of the degree of absorption and spans the range between 1 and 0, with 1 and 0 meaning purely scattering and purely absorbing media, correspondingly,  $P(\mu, \phi; \mu', \phi')$  is the phase function and represents the angular pattern of the scattered radiation.

The source term in Eq. (2.1) has a form

$$S(\tau, \mu, \phi) = \frac{\omega}{4\pi} F_0 P(\mu, \phi; \mu_0, \phi_0) \exp(-\tau / \mu_0) + (1 - \omega) B(T), \quad (2.2)$$

where  $F_0$  is the monochromatic solar flux at the top of the atmosphere,  $\mu_0 = \cos(\theta_0)$ ,  $\theta_0$  and  $\phi_0$  are the zenith and azimuth angles at which the solar radiance illuminates the top of the atmosphere. The second term of the source function,  $S(\tau, \mu, \phi)$ , represents the contributions of longwave radiation which can be described by the Planck function. Since 2B-TAU algorithm uses MODIS reflectivities, we can set  $F_0 = \pi$ .

The solution of (2.1) is subject to the standard boundary conditions. They describe radiance interaction with the surface at the bottom of the atmosphere.

### 2.2.2 Method of solution of the RTE

The selected algorithm uses a multi-stream plane-parallel adding model. This method is based on a discretization of the equation of transfer so that the Eq. (2.1) is represented in a discrete ordinate form and then the adding method is applied to obtain the solution. We decompose  $I(\tau, \mu', \phi')$ , and  $S(\tau, \mu, \phi)$  over the azimuthal coordinate  $\phi$  using Fourier series. The functions are decomposed over the zenith coordinate  $\mu$  using numerical quadrature (i.e. Gaussian). The phase function  $P(\mu, \phi; \mu', \phi')$  is represented as a series of the Legendre polynomials. Our model assumes that clouds can be represented as plane-parallel entities comprised of water or ice, and hence, our atmosphere can be divided into homogeneous layers. In this case, the radiances can be calculated by employing the interaction principle repeatedly to all layers resulting in a variation of the well known adding method. The global reflection, transmission matrices and source functions required by the adding method are calculated using an eigenmatrix technique described in [3],[4]. This method differs from the doubling method in that the global operators (i.e. the reflection ( $R$ ) and transmission ( $T$ ) matrices) also used in the construction of the source functions can be computed for any optical depth directly using formulas that do not require iteration. By contrast, doubling procedure is initialized by an infinitesimal generator and uses thereafter repeated matrix-to-matrix multiplications to

calculate the global operator associated with a given optical depth. As demonstrated by Cristi and Gabriel [3] this method is computationally efficient and stable.

### 2.2.3 Implementation details:

The forward model is implemented as follows:

1. Because of the solar radiance is a directional source and any value of the observation and solar illumination angles is possible, it may be required to take into account several azimuthal harmonics to achieve a required accuracy of the radiance estimation. This number generally increases when the observation and solar illumination angles become larger. Our numerical experiment shows that four harmonics are enough for most cloud scenes.
2. For the far infrared channels (wavelength greater than 3  $\mu\text{m}$ ), since the thermal sources are angularly isotropic, only the zero azimuth harmonic is required regardless of the observation geometry.
3. The expansion over  $\mu$  uses 8 angles up and 8 angles down. Correspondingly, the number of the expansion terms in the Legendre polynomial decomposition of the phase function is set to 16.
4. The measurement of the TOA reflectivities at two wavelengths to infer both  $\tau$  and  $r_{ef}$  is necessary.
5. A Lambertian surface is assumed. The surface albedo depends on geographical location and the day of the year and obtained from a datafile.
6. The phase function depends on the cloud constituent type. For the liquid water cloud, we assume that cloud particles have the spherical shape and their size distribution,  $p(r)$ , is described by the gamma distribution

$$p(r) = r^{k-1} \frac{\exp(-r/b)}{\Gamma(k)b^k}, \quad (2.3)$$

where  $\Gamma(k)$  is the Gamma function.

For the ice water cloud the model suggested by Yang et al [5] is used.

7. The single scattering albedo and coefficients of phase function decomposition into the Legendre polynomials are pre-calculated and organized as look up tables.

## 2.3 Bayesian Retrieval

The general approach of the retrieval is as shown in Figure 2, starting with process 5 (Estimate  $\bar{x}_{prior}$ ) and ending with process 8 (Eval QC flags). In general, for each cloudy profile produced by the CPR, an *a priori* estimate of the column vector containing cloud optical and effective radius is supplied. The estimates are updated until the forward-modeled reflectivities produced by the estimates are in agreement with the observed reflectivities obtained from MODIS, subject to the uncertainties in both the *a priori* estimates and in the MODIS reflectivities.

### 2.3.1 *a priori* Estimates

Initial estimates (*a priori* estimates) of column cloud optical depth and effective radius are required for the retrieval. If the CPR indicates the column is cloudy, the radar reflectivity profile is used to produce the *a priori* estimate. Each radar range gate is assumed to hold liquid or ice exclusively. Using a fixed temperature defining the phase transition (253 K), the ECMWF-AUX temperature profile is used to determine the water phase contained in each range gate. The auxiliary datasets (IWC-RO-AUX and CWC-RO-AUX) are used to provide information about the liquid/ice water contents for the each range gate. The water contents are then converted to the optical depths using the anomalous diffraction theory (Mitchell and Arnott [6]). The effective radius is the same as that used in the CPR to obtain the optical depth.

If a column is indicated cloudy by the MODIS scene characterization obtained from 2B-GEOPROF but the CPR does not indicate cloud, the *a priori* optical depth and effective radius are estimated by decoding the MODIS scene characterization and assigning the values which are typical to the characterization.

### 2.3.2 MODIS Reflectivities and Uncertainties

A subset of MODIS reflectivities and uncertainties are obtained from the MODIS level 1B radiance product. The subset consists of a 3x5 grid of MODIS pixels for each CloudSat profile. A vector of MODIS reflectivities values (0.864  $\mu\text{m}$  and 2.13  $\mu\text{m}$  for day time retrieval; 3.7  $\mu\text{m}$  and 11.0  $\mu\text{m}$  for night time retrieval) and a vector of reflectivity uncertainties are associated with each pixel. For each CloudSat profile, a simple mean is taken of the valid reflectivity and uncertainty values over this 3x5 grid.

### 2.3.3 Iteration and Convergence

The framework for iteratively updating the state vector  $\bar{x}$  containing the cloud optical depth and effective radius and testing for convergence is similar to that described by Marks and Rodgers [2] and by Rogers [7]. The expression for the updated value of  $\bar{x}$  is given by (adapted from Eq. (5.9) of Rodgers [7]) is:

$$\bar{x}_{i+1} = \bar{x}_i + [\mathbf{S}_a^{-1} + \mathbf{K}_i^T \mathbf{S}_e^{-1} \mathbf{K}_i]^{-1} \mathbf{K}_i^T \mathbf{S}_e^{-1} [\bar{I}_e - \bar{I}(\bar{x}_i) + \mathbf{K}_i (\bar{x}_i - \bar{x}_a)], \quad (2.4)$$

where the subscript *a* refers to *a priori* values, the subscript *e* refers to the measured values, and the subscripts *i*, *i*+1 refer to the iteration cycle number. In Eq. (2.4)  $\bar{x}$  is the column state vector containing the optical depth and effective radius, and  $\mathbf{K}$  is the Jacobian matrix:

$$\mathbf{K} = \begin{pmatrix} \left. \frac{dI}{d\tau} \right|_{\lambda_1} & \left. \frac{dI}{dr_{eff}} \right|_{\lambda_1} \\ \left. \frac{dI}{d\tau} \right|_{\lambda_2} & \left. \frac{dI}{dr_{eff}} \right|_{\lambda_2} \end{pmatrix} \quad (2.5)$$

The matrices  $\mathbf{S}_a$  and  $\mathbf{S}_e$  refer to uncertainties in the *a priori* state vector,  $\bar{x}_a$ , and MODIS reflectivities,  $\bar{I}_e$ , respectively, and can be written as follow:

$$\mathbf{S}_a = \begin{pmatrix} \sigma_\tau & 0 \\ 0 & \sigma_{r_{\text{eff}}} \end{pmatrix} \quad \text{and} \quad \mathbf{S}_e = \begin{pmatrix} \sigma_{I_{\lambda_1}} & 0 \\ 0 & \sigma_{I_{\lambda_2}} \end{pmatrix} \quad (2.6)$$

Acceptable convergence is achieved when (Eqs. (5.29, 5.31) of Rodgers [7]):

$$d = \left\{ \mathbf{K}_i \mathbf{S}_e^{-1} [\bar{I}_e - \bar{I}(\bar{x})] - \mathbf{S}_a^{-1} [\bar{x}_i - \bar{x}_a] \right\} \ll 2 \quad (2.7)$$

The parameter  $d$  is an estimate of the  $\chi^2$  statistic for the retrieval.

In practice, the *a priori* estimate of the cloud column vector  $\bar{x}_a$  is used as the starting value (i.e.,  $\bar{x}_0 - \bar{x}_a$ ). The Jacobian  $\mathbf{K}$  is evaluated using a numerical forward-difference approximation. The iterations are continued until either convergence is achieved or until the maximum number of iterations is reached.

### 3 Algorithm Inputs

#### 3.1 CloudSat

##### 3.1.1 CloudSat Level 2B Geometric Profile

Specific input requirements (Table 1 and 2) are time, geolocation (latitude, longitude, elevation), radar reflectivity, likelihood of hydrometeors, CPR cloud mask, MODIS scene characterization, CPR echo top characterization, CPR data status, surface bin number, spacecraft altitude, range to first bin and ray header range bin size. The parameter "nbin" is the number of vertical bins in the CloudSat radar profile [8].

Table 1a: Inputs from 2B-GEOPROF (per profile)

Variable Name	Dimensions	Range	Units	Description
<i>modis-scene</i>	Scalar	0 -9		MODIS scene characterization
<i>CPR-echotop</i>	Scalar	0-5		CloudSat echo top characterization
<i>CPR-cloudmask</i>	Nbin	0,1		CloudSat cloud mask
$Z_r$	Nbin	0.	dBZ	CPR reflectivity
<i>Profile_time</i>	Scalar	0-6000	s	Time since the start of the granule
<i>Latitude</i>	scalar	-90 -+90	deg	latitude
<i>Longitude</i>	scalar	-180/+180	deg	longitude
<i>Height</i>	Nbin	-5000- 30000	m	Height of range bin in Reflectivity/Cloud Mask above reference surface (~ mean sea level).

Table 1b: Inputs from 2B-GEOPROF common for all profiles

Variable Name	Dimensions	Range	Units	Description
<i>TAI_start</i>	Scalar	0-6E8	s	TAI time for the first profile
<i>Vertical_binsize</i>	Scalar		m	effective vertical height of the radar range bin
<i>Data_status</i>	Scalar			Data status flags
<i>SurfaceHeightBin</i>	Scalar	1-125		Location of Surface Bin as determined by 1B CPR algorithm. The value here is shifted (as Height).

### 3.1.2 CloudSat IWC-RO-AUX and LWC-RO-AUX

Table 2: Inputs from IWC-RO-AUX and LWC-RO-AUX (per profile)

Variable Name	Dimensions	Range	Units	Description
$IO\_RO\_vis\_extinction\_coef$	Nbin	0 -10	1/km	Ice-only Radar-only Visible Extinction Coefficient
$IO\_RO\_vis\_ext\_coef\_uncertainty$	Nbin	0-250	%	Ice-only Radar-only Visible Extinction Coefficient Uncertainty
$LO\_RO\_vis\_extinction\_coef$	Nbin	0-90	1/km	Liqued-only Radar-only Visible Extinction Coefficient
$LO\_RO\_vis\_ext\_coef\_uncertainty$	Nbin	0-250	%	Ice-only Radar-only Visible Extinction Coefficient Uncertainty

## 3.2 Ancillary (Non-CloudSat)

### 3.2.1 CloudSat Ancillary Albedo Dataset

Specific input requirements (Table 3) are surface albedo [9]. The parameter "nchan" is the number of channels used to retrieve  $\tau$  and  $r_{eff}$ .

Table 3: Inputs from AN-ALBEDO (per profile)

Variable Name	Dimensions	Range	Units	Description
$A_s$	nchan	0. -1.	-	surface albedo

### 3.2.2 CloudSat Auxiliary MODIS Reflectivities

Specific input requirements (Table 4) are reflectivities and reflectivity uncertainty (See [10] for details). The parameter "nfoot" is the number of MODIS pixels subsetted to cover the CloudSat radar footprint.

Table 4: Inputs from MODIS-AUX (per profile)

Variable Name	Dimensions	Range	Units	Description
$\bar{I}_e$	nfoot, nchan	0. -?	$W / m^2 sr \mu m$	MODIS reflectivities
$\Delta \bar{I}_e$	nfoot, nchan	0. -?	$W / m^2 sr \mu m$	MODIS reflectivity uncertainties

### 3.2.3 CloudSat Auxiliary ECMWF Dataset

Specific input requirements (Table 5) are the temperature, specific humidity, and pressure profile as well as surface temperature and pressure. See [9].

Table 5: Inputs from ECMWF-AUX (per profile)

Variable Name	Dimensions	Range	Units	Description
$T$	nbin	0. -?	K	temperature profile
$P$	nbin	0. -?	Pa	pressure profile
$S_u$	nbin	0. -?	<i>Kg/Kg</i>	Specific humidity
$P_0$	scalar	0. -?	Pa	surface pressure
$T_0$	scalar	0. -?	K	surface temperature

### 3.3 Control and Calibration

TBD by 2B-TAU algorithm team.

## 4 Algorithm Implementation

### 4.1 Flowchart overview of the retrieval algorithm

See Figure 2.

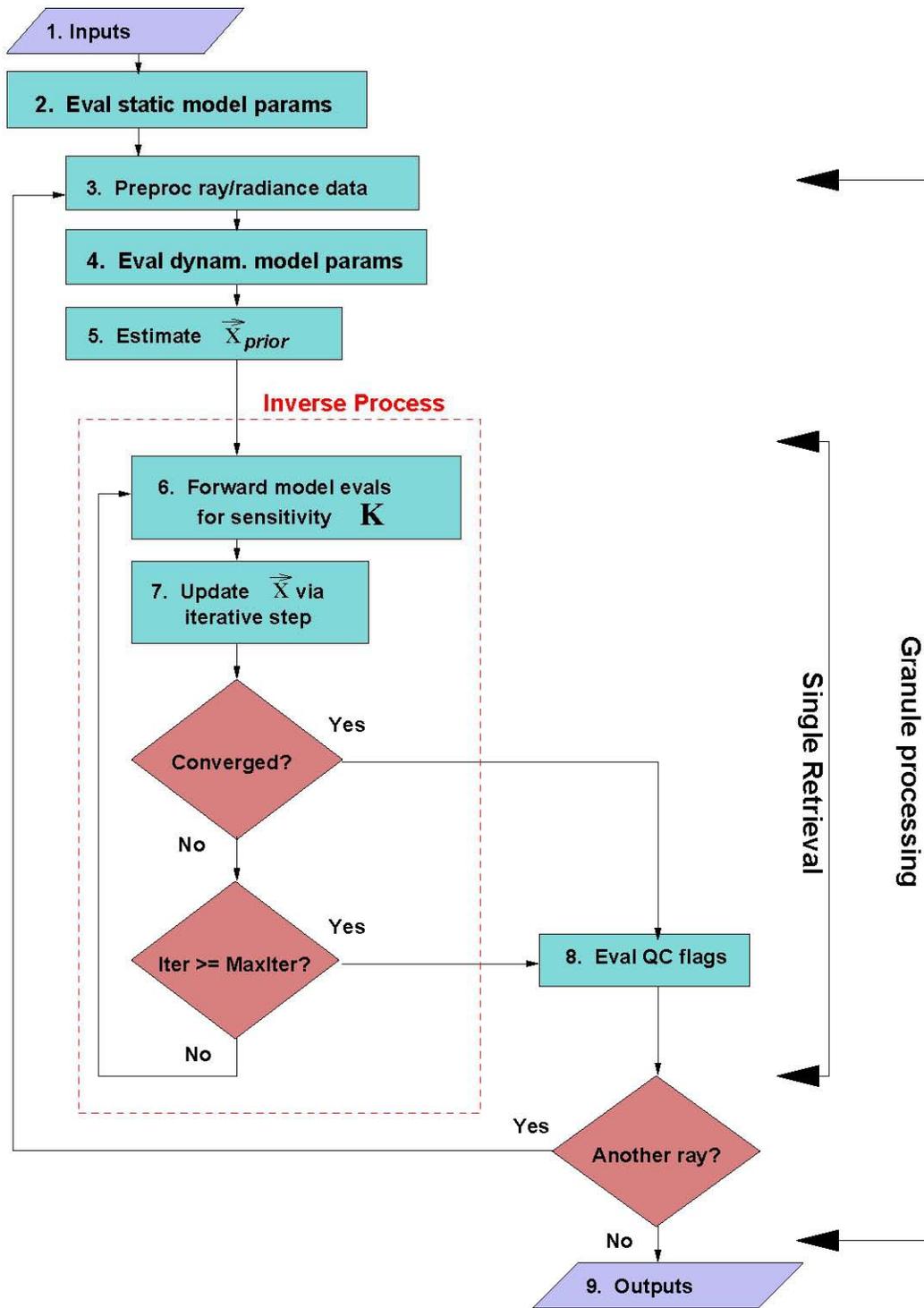


Figure 2: Retrieval process diagram

## 4.2 Pseudocode description

Following is a pseudocode description of the algorithm:

```
start 2B-TAU
open (2B-GEOPROF, 1B-CPR)
open ancillary data files (AN-ALBEDO, MODIS-AUX, ECMWF-AUX)
set TOA  $F_0 = \pi$ 
get (solar, sensor) zenith angle ( $SZA, SEZA$ ) (MODIS-AUX)
get (solar, sensor) azimuth angle ( $SAA, SEAA$ ) (MODIS-AUX)
for-each 2B-GEOPROF profile
    clear status
    if ( $SZA \leq SZA_{\max}$ ) OR ( $SZA > SZA_{\text{horiz}}$ ) perform the retrieval
        set status: daytime or nighttime
        read MODIS scene characterization (2B-GEOPROF)
        read CPR echo top characterization (2B-GEOPROF)
        eval status:scene
        if status:scene=not clear
            compute relative azimuth angle
            read CPR reflectivity profile
            read CPR cloud mask (2B-GEOPROF)
            read ECMWF (temperature, pressure, specific humidity and
            ozone) (ECMWF-AUX)
            compute gas absorption (correlated-k distribution)
            eval status:phase
            set prior effective radius (from cloud phase information)
            and uncertainty
            read surface albedo(AN-ALBEDO)
            read MODIS reflectivity data (MODIS-AUX)
            compute spatially-averaged MODIS reflectivity vector
            read prior optical thickness (IWC-RO-AUX and LWC-RO-AUX)
            compute  $\bar{x}_a$  and  $\mathbf{S}_a$ 
            set convergence parameter  $d$  to the initial value
            set iteration counter  $i = 0$ 
            set  $\bar{x}_i = \bar{x}_a$ 
            while ( $d > 1$  and  $i < i_{\max}$ )
                compute  $\bar{I}(\bar{x}_i)$ 
                compute  $\bar{I}(\tau_i + \delta\tau_i)$ 
                compute  $\bar{I}(r_{\text{eff},i} + \delta r_{\text{eff},i})$ 
                compute  $\mathbf{K}_a$ 
```

```

        compute  $\bar{x}_i$ 
        compute  $d$ 
        set  $i = i + 1$ 
end-while ( $d > 1$  and  $i < i_{\max}$ )
if  $i == i_{\max}$  (failed to converge)
    set  $\tau = \text{flagmissing}$ 
    set  $\tau(\text{bin}) = \text{flagmissing}$ 
    set  $r_{\text{eff}} = \text{flagmissing}$ 
    set  $\sigma_{\tau} = \text{flagmissing}$ 
    set  $\sigma_{r_{\text{eff}}} = \text{flagmissing}$ 
    set  $d = \text{flagmissing}$ 
    set  $\text{status} = \text{no\_converge}$ 
else
    set  $\tau = \tau_i$ 
    compute  $\sigma_{\tau}$  (uncertainty in retrieved optical depth)
    compute  $r_{\text{eff}}$ 
    compute  $\sigma_{r_{\text{eff}}}$  (uncertainty in retrieved effective
radius)
    compute  $\tau(\text{bin})$  (vertical profile of cloud optical
depth)
    set  $d = d_i$ 
    set  $\text{status} = \text{converge}, \text{status} = \text{prior}$ 
end-if ( $i == i_{\max}$ )
else ( $\text{status} = \text{scene} = \text{clear}$ )
    set  $\tau = \text{flagclear}$ 
    set  $\tau(\text{bin}) = \text{flagclear}$ 
    set  $r_{\text{eff}} = \text{flagclear}$ 
    set  $\sigma_{\tau} = \text{flagclear}$ 
    set  $\sigma_{r_{\text{eff}}} = \text{flagclear}$ 
    set  $d = \text{flagclear}$ 
end-if ( $\text{status} = \text{scene} = \text{not clear}$ )
else ( $SZA > SZA_{\max}$ ) OR ( $SZA < SZA_{\text{horiz}}$ ) no retrieval
    set  $\tau = \text{flagmissing}$ 
    set  $\tau(\text{bin}) = \text{flagmissing}$ 

```

```
        set  $r_{eff}$  =flagmissing
        set  $\sigma_{\tau}$  =flagmissing
        set  $\sigma_{r_{eff}}$  =flagmissing
        set  $d$  =flagmissing
    end-if (SZA<SZAmax)
end-for-each (2B-GEOPROF profile)
compute scaled  $\tau$ ,  $r_{eff}$ ,  $\sigma_{\tau}$ ,  $\sigma_{r_{eff}}$ ,  $\tau(bin)$ , and  $d$ 
open 2B-TAU output file
write status, scaled  $\tau$ ,  $r_{eff}$ ,  $\sigma_{\tau}$ ,  $\sigma_{r_{eff}}$ ,  $\tau(bin)$ , and  $d$ 
close 2B-TAU output file
close 2B-GEOPROF
close ancillary data files
stop 2B-TAU
```

### 4.2.1 Algorithm Parameters

See Table 6. The parameter "npara" is the dimension of the retrieved vector  $\bar{x}_i$

Table 6: Algorithm Parameters (per profile)

Variable Name	Dimensions	Range	Units	Description
$SZA, SEZA$	scalar	0. - 180°	degrees	solar, sensor zenith angle
$SAA, SEAA$	scalar	-180° -180°	degrees	solar, sensor azimuth angle
$SZA_{max}$	scalar	80°	degrees	maximum solar zenith angle
$SZA_{horiz}$	scalar	90°	degrees	horizon solar zenith angle
$\bar{I}_e$	nchan	0. -?	$W / m^2 sr \mu m$	vector of MODIS reflectivities
$S_e$	nchan, npara	0. -?	$W / m^2 sr \mu m$	matrix of MODIS reflectivity uncertainty
$\bar{x}_a$	npara	0. -?	-	<i>a priori</i> cloud column vector
$S_a$	npara, npara	0. -?	-	matrix of <i>a priori</i> cloud parameters uncertainty
$i$	scalar	0 - $i_{max}$	-	iteration counter
$i_{max}$	scalar	-	-	maximum allowed iterations
$\bar{x}_i$	npara	0. -?	-	state vector
$\bar{I}(\bar{x}_i)$	nchan	0. -?	$W / m^2 sr \mu m$	simulated reflectivities
<i>flagmissing</i>	scalar	-99.	-	fill value for missing results
<i>flagclear</i>	scalar	0.	-	fill value for clear-sky results

### 4.3 Timing requirements

As retrievals are to be performed in real time, the requirement on the computational speed of the algorithm is estimated from the following considerations:

- 14.6 orbits/day;
- approximately 40,000 profiles per orbit (day and night) .

This gives around 584,000 profiles to process per day and sets an upper time constraint, given no other requirements, of 0.15 seconds per retrieval. However the number of cloudy profiles should be of the order of 2/3 of the total number of profiles, i.e. around 390,000 which gives a realistic time constraint of 0.22 seconds. As other products are dependent on the optical depth retrievals, the maximum time constraint will be significantly smaller. The actual performance of the version 3 of 2B-TAU, tested on the Test Data Set 3, is around 0.2 seconds per retrieval on a Pentium 4 (3.2Ghz) computer.

## 5 Data Product Output Format

### 5.1 Data Contents

The data specifically produced by the 2B-TAU algorithm are described in Table 7.

Table 7: Algorithm Outputs (per profile)

Variable Name	Dimensions	Range	Units	Description
$\tau$	scalar	0.-200	-	total cloud column optical depth
$r_{eff}$	scalar	0.-200	-	cloud column effective radius
$\sigma_{\tau}$	scalar	0.-200	-	scaled standard deviation of $\tau$
$\sigma_{r_{eff}}$	scalar	0.-200	-	scaled standard deviation of $r_{eff}$
$d$	scalar	0.-100	-	$\chi^2$ estimate
$\tau(bin)$	nbins	0.-200	-	distributed column optical depth
<i>status</i>	scalar	0-127	-	retrieval mode and status

### 5.2 Data Format Overview

In addition to the data specific to the 2B-TAU algorithm results, the HDF-EOS data structure may incorporate granule data/metadata (describing the characteristics of the orbit or granule) and supplementary ray data/metadata. The data structure is described in Table 8. Only those common data fields specifically required by the 2B-TAU algorithm are listed in the table and included in the descriptions in section 5.3. The entries in the "Size" column of the table represent the array size where appropriate (*e.g.*, nray), the variable type (REAL, INTEGER, CHAR) and the size in bytes of each element (*e.g.*, (4)). The parameter "nray" is the total number of profiles in the granule.

Table 8: HDF-EOS File Structure

Structure/Data Name				Size
Data Granule	Granule Metadata			TBD
	Granule Data			TBD
	Swath Metadata	Common metadata	TBD	TBD
		2B-TAU metadata	$\tau$ offset	1*REAL(4)
			$\tau$ scale factor	1*REAL(4)
			$r_{eff}$ offset	1*REAL(4)
			$r_{eff}$ scale factor	1*REAL(4)
			$d$ offset	1*REAL(4)

			$d$ scale factor	1*REAL(4)
			$\tau(bin)$ offset	1*REAL(4)
			$\tau(bin)$ scale factor	1*REAL(4)
	Swath Data	Common data fields	frame counter	nray*INTEGER(2)
			UTC time	nray*INTEGER(10)
			status flag	nray*INTEGER(2)
			geolocation latitude	nray*REAL(4)
			geolocation longitude	nray*REAL(4)
			DEM elevation	nray*REAL(4)
		2B-TAU data fields	$\tau$	nray*INTEGER(2)
			$\sigma_{\tau}$	nray*INTEGER(2)
			$r_{eff}$	nray*INTEGER(2)
			$\sigma_{r_{eff}}$	nray*INTEGER(2)
			$d$	nray* INTEGER(2)
			$\tau(bin)$	nray*nbin*INTEGER(2)
			<b>status</b>	nray*INTEGER(1)

### 5.3 Data Descriptions Granule Metadata (attributes, size TBD by CIRA)

#### Granule Data (attributes, size TBD by CIRA)

#### 2B-TAU data fields:

$\tau$  (SDS, nray\*INTEGER(2))

Cloud column optical depth scaled to two-byte integer

$r_{eff}$  (SDS, nray\*INTEGER(2))

Cloud column effective radius scaled to two-byte integer

$\sigma_{\tau}$  (SDS, nray\*INTEGER(2))

Fractional uncertainty in cloud column optical depth scaled to two-byte integer

$\sigma_{r_{eff}}$  (SDS, nray\*INTEGER(2))

Fractional uncertainty in cloud column effective radius scaled to two-byte integer

$d$  (SDS, nray\*INTEGER(2))

$\chi^2$  estimate for retrieval of  $\tau$  scaled to two-byte integer

$\tau(bin)$  (SDS, nray\*nbin\*INTEGER(2))

Cloud layer optical depths scaled to two-byte integer

**status** (SDS, nray\*INTEGER(1)) A one-byte (8 bit) status flag with six bits allocated as follows and two bits unallocated (bits numbered right to left):

*status:scenemodis*

bit 0: 0=clear, 1=cloudy-MODIS

*status:scenecloudsat*

bit 1: 0=clear, 1=cloudy-CloudSat

*status:missing:*

bit 2: 0=missing values from inputs or  $SZA_{\max} < SZA < SZA_{\text{horiz}}$ ,  
1=no missing value from inputs

*status:phase:*

bit 3: 0=liquid, 1=ice

*status:converge:*

bit 4: 0=not converged, 1=converged

*status:prior:*

bit 5: 1=retrieval dominated by *a priori* information, 0=retrieval dominated by data

*status:sun:*

bit 6: 0=nighttime retrieval, 1=daytime retrieval

*status:channel:*

bit 7: 0=both reflectivities available (retrieve  $\tau$  and  $r_{\text{eff}}$ ), 1=one reflectivity is missing  
(retrieve  $\tau$  only)

## **2B-TAU metadata fields:**

$\tau$  **offset** (SDS attribute, REAL(4))

The offset used to rescale  $\tau$ .

$\tau$  **scale factor** (SDS attribute, REAL(4))

The scale factor used to rescale  $\tau$ .

$r_{\text{eff}}$  **offset** (SDS attribute, REAL(4))

The offset used to rescale  $r_{\text{eff}}$ .

$r_{\text{eff}}$  **scale factor** (SDS attribute, REAL(4))

The scale factor used to rescale  $r_{\text{eff}}$ .

$d$  **offset** (SDS attribute, REAL(4))

The offset used to rescale  $d$ .

$d$  **scale factor** (SDS attribute, REAL(4))

The scale factor used to rescale  $d$ .

$\tau(\text{bin})$  **offset** (SDS attribute, REAL(4))

The offset used to rescale  $\tau(\text{bin})$ .

$\tau(\text{bin})$  **scale factor** (SDS attribute, REAL(4))

The scale factor used to rescale  $\tau(bin)$ .

#### **Common data fields:**

**frame counter** ( nray\*INTEGER(2))

Sequential frame counter carried from Level 0 data

**UTC time** (nray\*INTEGER(10)) Frame (or ray) UTC time converted from VTCW time. A multiword record containing year, month, day of month, hour, minute, second, millisecond and day of year. See Li and Durden [11] for details.

**status flag** ( nray\*INTEGER(2))

Per email with D. Reinke. Attributes TBD by CIRA, other algorithms.

**geolocation longitude** (nray\*REAL(4))

The longitude of the center of the IFOV at the altitude of the earth ellipsoid (Li and Durden [11]).

**geolocation latitude** (nray\*REAL(4))

The latitude of the center of the IFOV at the altitude of the earth ellipsoid (Li and Durden [10]).

**DEM elevation** (nray\*REAL(4))

Surface elevation of the Earth at the geolocation longitude and latitude.

#### **Common metadata fields:**

No additional metadata are specifically required by the 2B-TAU algorithm.

### **6 Operator Instructions**

Quality assurance on the data (preliminary list):

Correlation of total optical depth versus total Z for columns where 2B-TAU retrievals are performed (scatter plot)

Frequency of occurrence/clustering of outliers of total optical depth

Frequency of occurrence/clustering of "failed to converge" flag

### **7 Acronym List**

<b>CIRA</b>	Cooperative Institute for Research in the Atmosphere
<b>CPR</b>	Cloud Profiling Radar
<b>EOS</b>	Earth Observing System
<b>HDF</b>	Hierarchical Data Format
<b>IFOV</b>	Instantaneous Field of View
<b>QC</b>	Quality Control
<b>MODIS</b>	Moderate Resolution Imaging Spectrometer
<b>SDS</b>	Scientific Data Set
<b>TAI</b>	International Atomic Time: seconds since 00:00:00 Jan 1 1993

<b>TOA</b>	Top of Atmosphere
<b>VTCW</b>	Vehicle Time Code Word
<b>BDRF</b>	Bidirectional Reflection Function

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